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A DIGITAL FILTER REPRESENTATION OF THE ASQ-81
MAGNETOMETER

by

Michael Charles Huete

September 1983

Thesis Advisor: Andrew R. Ochadlick

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A Digital Filter Representation of the ASQ-81
Magnetometer

by

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Submitted in partial fulfillment of the
requirements for the degree of

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ABSTRACT

A digital filter representation of the ASQ-81 magnetometer is derived from the s-plane transfer functions of the system through the use of a bilinear transformation. A FORTRAN computer program is written which applies this representation to time-sampled total magnetic field data in order to obtain a time series representation of ASQ-81 filtered total field. A series of simulations and a field experiment are conducted which verify the program output. Applications of this program include usage in conjunction with geomagnetic field data in order to produce a new data set representative of geomagnetic noise observed by Navy MAD (Magnetic Anomaly Detection) aircraft with the potential to investigate techniques of reducing geomagnetic noise in MAD aircraft.

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I. INTRODUCTION

The detection and location of submarines (and other magnetic bodies) through the discrimination of changes or anomalies in the Earth's magnetic field is called Magnetic Anomaly Detection or MAD. In this technique, a magnetometer measures the magnitude of the Earth's magnetic field and provides an indication of that magnitude, or, more usually, an indication of changes in the magnitude of the Earth's field. These changes, or anomalies, can indicate the presence of magnetized bodies which may or may not be a submarine.

The magnetometer currently in use in the United States Navy for use in this MAD process is the AN/ASQ-81 metastable helium vapor total field magnetometer.

Research is currently being conducted at the Naval Postgraduate School in Monterey, California, in various aspects of the applications of magnetometers, including Magnetic Anomaly Detection (MAD). Within the context of this research, magnetic field measurements are made through the use of sets of wire wound coils vice any specific magnetometer or magnetic detecting system. The data collected through the use of these coils is evaluated and

processed in a variety of methods for different project goals.

This thesis project is designed to produce an acceptable alternative to the physical presence of an experimental AN/ASQ-81 magnetometer at the postgraduate school by allowing the determination, in conjunction with other research in progress, of the output of the AN/ASQ-81 magnetometer from the data collected from the school's measurement coils. It is hoped that this will assist future research projects as, for example, in allowing a determination of environmental noise of such characteristics as to affect the AN/ASQ-81 magnetometer operationally with the eventual goal of providing an environmental noise index or a system of removing such noise from the magnetometer-detection system.

II. GEOMAGNETICS REVIEW

A. EARTH'S MAGNETIC FIELD

1. Constituents of the Geomagnetic Field

The most common method of specifying the constituting parts of the geomagnetic field is to divide the field in terms of distance from the center of the Earth. This method results in three classifications: internal, crustal, and external. [Ref. 1]

The internal field originates in the core region and is the most stable field, containing only extremely low frequency temporal variations. The crustal, or anomalous, field arises from modifications made on the internal field by materials and structures in the Earth's crust. These variations are not constant with regard to spatial locations, and comprise part of what is known as geological variations. The external field is the most dynamic and arises from many sources, including the interaction between the solar wind and the Earth's magnetic field.

In addition to this method of defining the Earth's magnetic field is the method of time variations. This method consists of considering that part of the field which varies with periodicities greater than about one year as the

steady field and everything else as the variation field.

[Ref. 2]

The steady field consists of the internal field, also referred to as the main field. Slow variations of the main field with periods of years or longer are referred to as secular variations.

There are various elements that contribute to the geomagnetic field, some of which are external to the Earth's surface. External contributions make up only a small part of the steady field, but play an important role in the variation field. These external sources include current systems in the Earth's upper atmosphere affected by solar electromagnetic radiation and gravitation, solar corpuscular radiation and the interaction of solar plasma with the main field, and the effect of the solar interplanetary field.

[Ref. 3]

The geomagnetic field changes with time. As previously mentioned, very slow variations in the main field with periods of on the order of years to thousands of years are referred to as secular variations. Secular variations are caused by a variation in the strength or orientation of the Earth's center dipole.

Other time variations of the field can be categorized into quiet variation fields and disturbed variation fields. Disturbed variation fields include geomagnetic micropulsations, which are of particular interest to

operational forces as these can mask target signatures and are therefore a source of noise to MAD sensors.

Quiet variation fields are those which are not due to disturbances in the interplanetary environment and which vary slowly and regularly. [Ref. 3]

Disturbed variation fields are geomagnetic field variations that appear to be the result of interplanetary environmental changes and do not possess a simple periodicity. These variations include ionospheric disturbances, the aurora, geomagnetic storms, and geomagnetic micropulsations.

2. Elements of the Magnetic Field Vector

The geomagnetic field vector is characterized at any point by its direction and magnitude. This is commonly accomplished through a system of coordinates as shown in Figure 2.1. The field is measured in terms of local coordinates with respect to true North. [Ref. 3]

The various coordinates are referred to as magnetic elements and are defined as follows:

B: Total field intensity (the symbol F is sometimes also used, as in this figure.)

H: Horizontal component

X: Northward, or NorthSouth component

Y: Eastward, or EastWest component

Z: Downward, or Vertical component

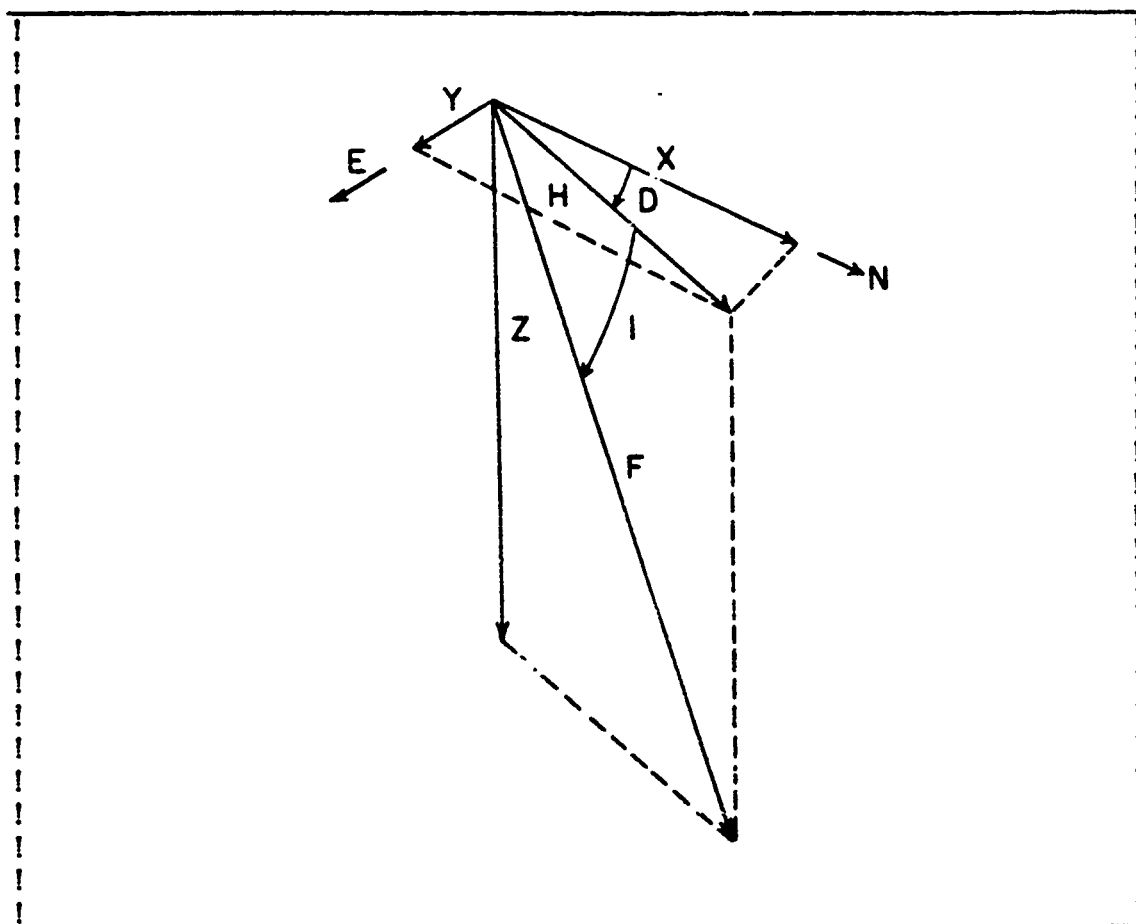


Figure 2.1 Magnetic Field Elements [Ref. 4].

D: Declination or magnetic variation

This is the angle between X and H and
is measured positive eastward.

I Inclination or Dip Angle.

This is the angle between H and B (or F)
and is measured positive downward.

III. THE AN/ASQ-81 MAGNETOMETER

A. DESCRIPTION OF SYSTEM OPERATION

The Magnetic Anomaly Detecting set currently in use in the U S Navy is the AN/ASQ-81 magnetometer. This set is used to locate and classify submerged submarines by sensing disturbances in the Earth's magnetic field (anomalies) caused by the presence of the magnetic mass of the submarine. The disturbance of the Earth's field is detected by the magnetometer, processed through filtering circuits, and amplified. The output signal of the magnetometer is displayed on a chart recorder for interpretation by an operator.

The magnetic detecting set is a metastable helium vapor magnetometer. The operation of the magnetometer is based on the light absorption properties of helium gas subjected to certain light stimulus (optical pumping), radio frequency excitation, and the Earth's magnetic field. The magnetometer consists of a helium lamp, lens and polarizer to generate a beam of polarized light radiation. This focused and polarized light beam is directed through a helium absorption cell to an infrared (IR) detector. Some of the helium gas in the absorption cell is maintained in a metastable state by application of VHF excitation.

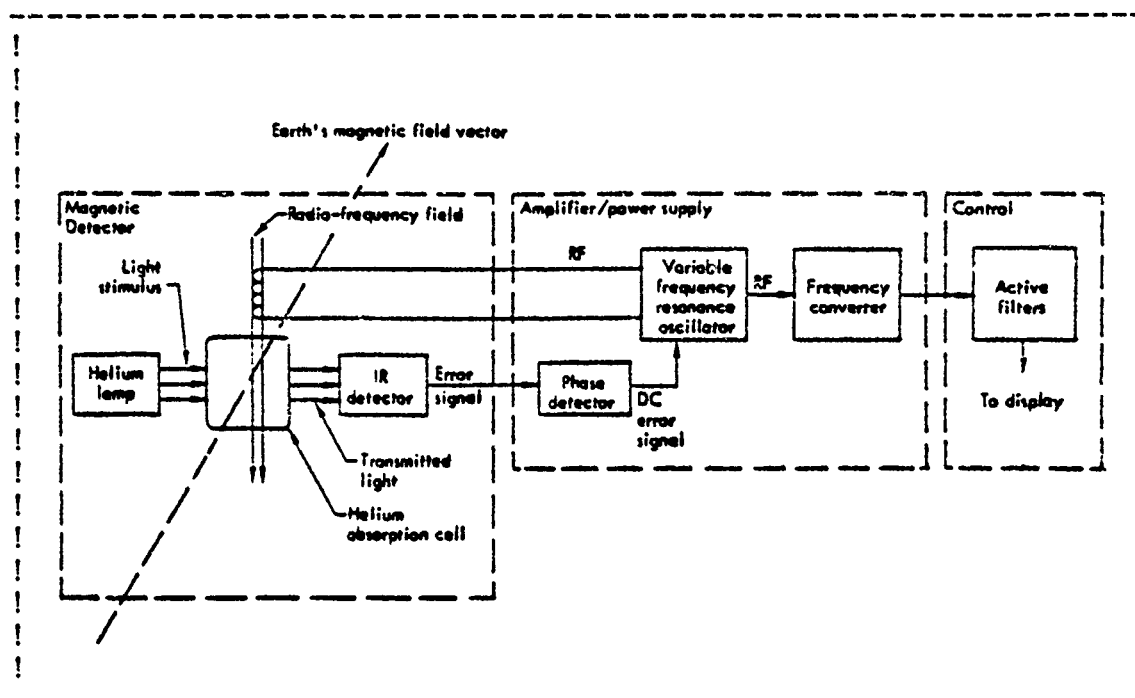


Figure 3.1 : Metastable Helium Magnetometer [Ref.5].

The Earth's magnetic field imposes a magnetic force upon the excited helium vapor atoms to force the atoms into one of three energy sublevels. This is called the Zeeman effect. The rate or frequency of atomic precession caused by this effect is called the Larmor frequency. A helium lamp is used to optically pump the atoms in the absorption cell, with the result that the polarized light energy passing through the absorption cell will polarize (magnetize) the helium atoms in the absorption cells by selectively pumping the Zeeman levels of the energy of the helium atoms in the cell. The magnetization direction is determined by the polarization of the photons from the helium lamp.

RF energy is then introduced to the absorption cell in the form of an additional magnetic field imposed through the use of coils oriented perpendicular to the precessed polarized helium atoms in the absorption cell and energized by a variable frequency RF oscillator. The RF oscillator is tuned to the Larmor frequency, which results in depolarization of the atoms. The atoms attempt to equally repopulate the Zeeman energy levels. However, the helium lamp is still beaming polarized light energy into the absorption cell, causing the atoms to absorb light energy and rise to an excited energy level. This absorption of light energy is detected through the use of an infrared detector. The RF oscillator frequency producing maximum light absorption is called the resonant frequency, and is determined through the use of a servo loop from the infrared detector to the RF variable frequency oscillator.

Therefore, any change in the Earth's magnetic field intensity will result in a change in the Larmor frequency of the helium atoms in the helium absorption cell. This new Larmor frequency will be detected by the ASQ-81 magnetometer. Since the gyromagnetic ratio of helium is 28.024 HZ per gamma, this detection of the resonant frequency provides a measurement of the Earth's magnetic field intensity at any given time. A change in the Earth's

magnetic field intensity could signal the presence of a submerged submarine.

The output resonant frequency developed by the magnetometer is converted to a proportional output voltage which is filtered through the Magnetic Anomaly Detection (MAD) bandpass filters for environmental noise reduction and utilized to drive a chart recorder for observation by an operator. [Ref. 6]

B. TRANSFER FUNCTIONS

Transfer functions for the AN/ASQ-81 filters were obtained from the manufacturer of the AN/ASQ-81 detecting set, Texas Instruments of Dallas, Texas. These transfer functions are listed in Appendix A and are in the form of $H(s)$, that is, the frequency domain, or S domain, where $S = j\omega$. The s -domain representation for transfer functions is routinely utilized to express output system characteristics for given system inputs. As the S domain representation is not utilized further in this discussion, it will not be further explained.

As the output signal of the ASQ-81 magnetometer is filtered through a fixed high-pass system, then through a selectable low pass system and a selectable high pass system (as shown in Figure 3.2 below), the transfer functions are listed in this order.

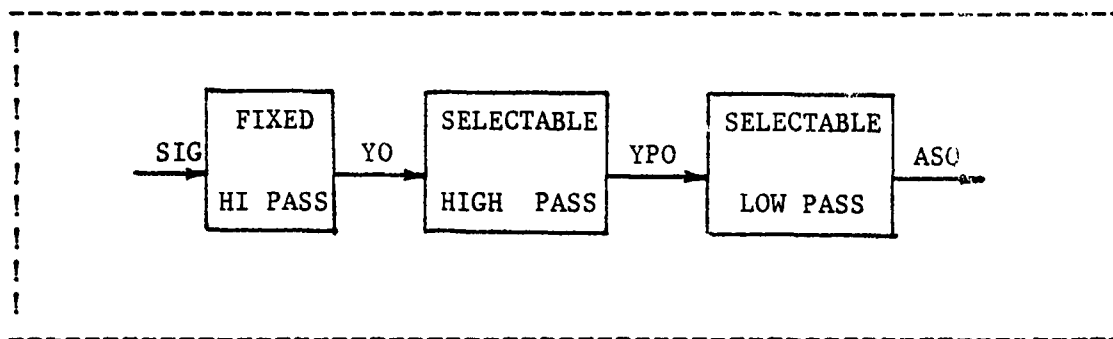


Figure 3.2 : Signal Flow Diagram for ASQ-81

Further discussion will be made of the selectable filters later.

IV. DIGITAL FILTERING MODELLING OF SYSTEMS

A. SEQUENCE REPRESENTATION OF TIME FUNCTIONS

1. Signal Representation

A signal can be defined as a function that conveys information, generally about the state or behavior of a physical system. Although signals can be represented in many ways, the information conveyed by the signal is contained in a pattern of variations of some form. Signals are represented mathematically as functions of one or more independent variables, one of the most common of which is time.

The independent variable of the mathematical representation of a signal may be continuous or discrete. Continuous time signals are signals that are defined over continually values of time and are therefore represented by continuous-variabled functions. Discrete time signals are defined at discrete time intervals and are therefore represented by functions whose independent variable(s) take on discrete values only. Discrete-time signals are represented as sequences of numbers. [Ref. 7]

In addition to the fact that the independent variables can be either continuous or discrete, the signal amplitude can be either continuous or discrete. Digital

signals are those for which both time and amplitude are discrete. Analog signals are those for which both time and amplitude are continuous.

Digital signal processing deals with transformations of signals that are discrete in both time and amplitude, usually represented by sequences of numbers. The nth number in the sequence x being processed is usually represented as x(n), and is formally written as:

$$x = [x(n)], \quad -\infty < n < +\infty$$

In general, an arbitrary sequence can be expressed as

$$x(n) = \sum_{k=-\infty}^{\infty} x(k) d(n-k)$$

where $d(n-k)$ is the unit sample at time k . In other words, an arbitrary sequence may be expressed as a sum of scaled, shifted unit samples, where the scaling factor is equal to the amplitude of the sequence at that time.

2. Linear Shift-Invariant Systems

A system is defined mathematically as a unique transformation or operator that maps an input sequence $[x(n)]$ into an output sequence $[y(n)]$. This is denoted as:

$$y(n) = T[x(n)]$$

and is often depicted as in Figure 4.1.

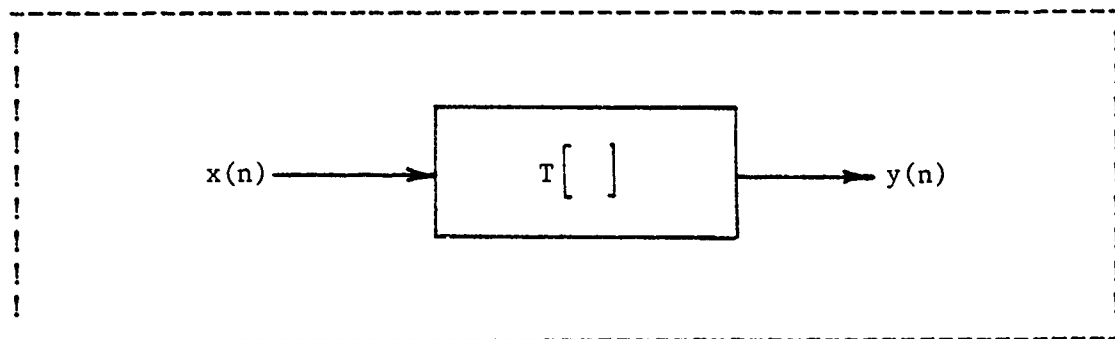


Figure 4.1: Representation of Transformation of an Input Sequence to an Output Sequence. [Ref.7]

Classes of discrete time systems are defined by placing constraints on the transformation $T[\]$.

The class of linear systems is defined by the principle of superposition. If $y_1(n)$ and $y_2(n)$ are the responses when $x_1(n)$ and $x_2(n)$ are the inputs, then a system is linear if

$$\begin{aligned} T[ax_1(n) + bx_2(n)] &= aT[x_1(n)] + bT[x_2(n)] \\ &= ay_1(n) + by_2(n) \end{aligned}$$

for any arbitrary constants a and b . This, together with the concept of representing a sequence by a sum of delayed and scaled unit-sample sequences, suggests that a linear system can be characterized by its unit-sample response. Specifically, let $h_k(n)$ be the response of the system to $d(n-k)$, a unit sample occurring at $n=k$. Then

$$y(n) = T\left[\sum_{k=-\infty}^{\infty} x(k) d(n-k)\right] \quad \text{or,}$$

$$y(n) = \sum_{k=-\infty}^{\infty} x(k) T[d(n-k)] = \sum_{k=-\infty}^{\infty} x(k) h_k(n)$$

Thus the system response can be expressed in terms of the response of the system to $d(n-k)$.

The class of shift invariant systems is characterized by the property that if $y(n)$ is the response to $x(n)$, then $y(n-k)$ is the response to $x(n-k)$, where k is a positive or negative integer. When the index n is associated with time, shift-invariance corresponds to time-invariance. The property of shift invariance implies that if $h(n)$ is the response to $d(n)$, then the response to $d(n-k)$ is simply $h(n-k)$. Therefore

$$y(n) = \sum_{k=-\infty}^{\infty} x(k) h(n-k)$$

and any linear shift-invariant system is completely characterized by its unit-sample response $h(n)$.

A subclass of linear shift-invariant systems consists of those systems for which the input $x(n)$ and the output $y(n)$ satisfy an N th-order linear constant-coefficient difference equation of the form

$$\sum_{k=0}^N a_k y(n-k) = \sum_{r=0}^M b_r x(n-r)$$

If the assumption of causality is made about the system, a linear difference equation provides an explicit relationship between the input to the system and the output of the system. This can be seen by rewriting the previous equation as

$$y(n) = \sum_{k=1}^N c_k y(n-k) + \sum_{r=0}^M d_r x(n-r)$$

where $c_k = -a_k / a_0$ and $d_r = b_r / a_0$.

Thus the n th value of the output can be computed from the n th value of the input and the N and M past values of the output and input, respectively. The difference equation not only represents the system for theoretical purposes, but it may also serve as a computational realization of the system. The z -Transform makes use of this property to realize systems.

B. THE z -TRANSFORM

1. Description of the z -Transform

The z -transform plays an important role in the analysis and representation of discrete-time linear shift-invariant systems. The z -transform, $X(z)$, of a sequence $x(n)$ is defined as

$$X(z) = \sum_{n=-\infty}^{\infty} x(n) z^{-n}$$

where z is a complex variable. This representation of the z -transform is referred to as the two-sided z transform. The one sided z -transform consists of the same summation for terms of n greater than or equal to zero. For the case that $x(n)=0$ for $n<0$, the one sided and two sided z transforms are equivalent.

By expressing the complex variable z in polar form as $z = re^{j\omega}$, the z -transform can be interpreted as the Fourier transform of $x(n)$ multiplied by an exponential sequence. For $r = 1$, that is, for $|z| = 1$, the z -transform is equal to the Fourier transform of the sequence.

2. The Bilinear Transformation

The transfer functions of analog systems are most often expressed in terms of $s = j\omega$ (see section III B.). This corresponds to the analog frequency response of the system. This analog frequency response can be "mapped", that is, transformed to the z -plane from the s -plane through the use of the bilinear transformation. The effect of utilizing the bilinear transformation is to convert a system transfer function in terms of the variable S into the system transfer function in terms of the variable z . The transformation itself is:

$$s = \frac{2}{T} \frac{1 - z^{-1}}{1 + z^{-1}}$$

and

$$z = \frac{(2/T) + s}{(2/T) - s}$$

where T is the sampling period, that is, the time between data samples.

Thus a transform can be made from one plane to the other. In this manner, the transfer function, $H(z)$, of a system may be obtained.

The bilinear transformation equations may be shown to hold in general, and the use of this transformation may be shown to yield stable digital filters from stable analog filters [Ref. 7]. The bilinear transformation maps the imaginary $j\omega$ axis in the s -plane onto a unit circle (of the region of convergence) in the z -plane, with the left half s -plane mapped onto the region inside the circle and the right hand (region of instability) s -plane mapped onto the region outside this circle [Ref. 8]. A complete discussion of the z -transform is available in several texts, some of which are listed in the Bibliography.

C. THE DIGITAL COMPUTATIONAL ALGORITHM

In implementing a digital filter on a digital computer such as the IBM 3033, the input-output relationship of the signals through the system being synthesized must be converted to a computational algorithm. The algorithm is specified in terms of a set of basic computations of elements. For the implementation of discrete-time systems

described by linear constant coefficient difference equations, such as the AN/ASQ-81, it is convenient to choose as these elements the basic operations of addition, delay, and multiplication by a constant. The computational algorithm for implementing the filter is then defined by a structure or network consisting of an interconnection of these basic operations. For a system transfer function of the form

$$H(z) = \frac{\sum_{k=0}^M b_k z^{-k}}{1 - \sum_{k=1}^N a_k z^{-k}} = \frac{Y(z)}{X(z)}$$

the difference equation relating input and output is easily written down directly from the system function and is given by

$$y(n) = \sum_{k=1}^N a_k y(n-k) + \sum_{k=0}^M b_k x(n-k) \quad [\text{Ref. 7}]$$

This difference equation can be interpreted directly as a computational algorithm in which the delayed values of the input are multiplied by the coefficients b_k , the delayed values of the output are multiplied by the coefficients a_k , and the resulting products are added. It is now easy to see the process to be followed in obtaining the computational algorithm for the AN/ASQ-81 magnetometer

transfer function. The z-transform of the system transfer function is obtained through the use of the bilinear transformation, and is then converted into a difference equation relating input and output signals, thence to a FORTRAN computer program. A table of z-transforms of system functions is included in Appendix B.

In the FORTRAN computer program realization of the total system computational algorithm, each filter block is transformed into a separate difference equation and algorithm. This was done to enable a "building block" type approach to the program, and to minimize computational and roundoff errors.

D. THE CASCADE FORM OF THE COMPUTATIONAL ALGORITHM

Even though the direct form realization of the digital filter design may be perfectly satisfactory in a theoretical sense, it may be less than desirable in the context of realization through the use of a general purpose computer of fixed register length. The parameters of a digital filter are usually obtained with a high degree of accuracy, which results in a faithful realization of the desired system. When these parameters are quantized, as in a finite memory register within a computer, the frequency response of the resulting digital filter may differ appreciably from the original design. In fact, the quantized filter may fail to

meet design specifications although the unquantized filter does. [Ref. 7]

The sensitivity of the filter response to errors in the filter parameters is dependent upon the structure of the filter realization. Therefore, in the event of an unacceptable change in the frequency response of the filter due to quantization errors, it is often possible to minimize the effect of these errors through an alternate filter realization structure. An alternate structure to the previously discussed direct form realization is the cascade form realization.

The direct form network structures were obtained directly from the system function $H(z)$ written in the form of a ratio of sums. If this ratio is factored into a product of polynomials of the form

$$H(z) = A \prod_{k=1}^{[(N+1)/2]} \frac{1 + B_{1k} z^{-1} + B_{2k} z^{-2}}{1 - a_{1k} z^{-1} - a_{2k} z^{-2}}$$

this product represents a general distribution of poles and zeros and suggests a set of structures consisting of a cascade of first and second-order subsystems. There is considerable freedom in the design of the subsystems, but it is best to realize the systems using a minimum of storage.

The expression of $H(z)$ in this form indicates the presence of poles and zeros in pairs. If poles and zeros

are not present in pairs, one of the coefficients B_{2k} or a_{2k} will be zero as appropriate. An implementation of such a cascade structure with the use of minimum memory can be obtained through a direct form II realization of each second order subsystem using techniques similar to the direct form implementation utilized previously. A cascade realization of a sixth-order system, such as the ASQ-81 system, using a direct form II realization of each second order subsystem would appear as in Figure 4.2 below.

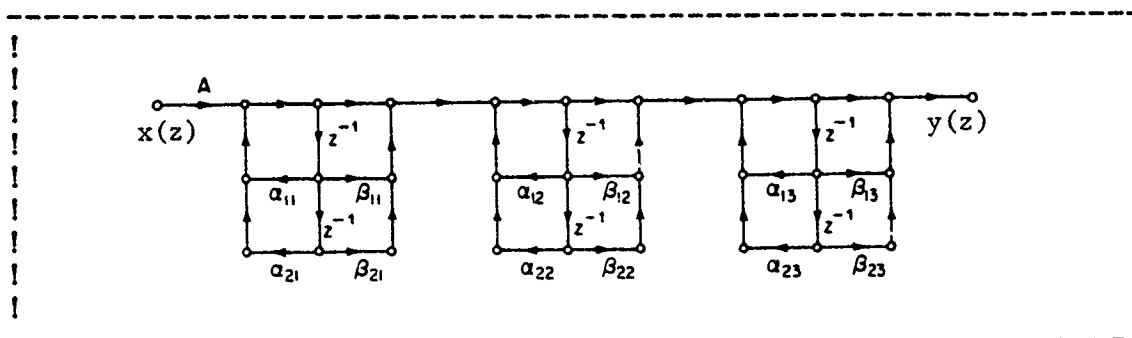


Figure 4.2: Cascade Structure With a Direct Form II Realization of Each Second Order Subsystem. [Ref. 7]

There is, theoretically, considerable flexibility in the manner in which the poles and zeros are paired together and in the order in which the resulting second-order subsystems are cascaded. However, although all such pairings and orderings are equivalent for infinite-precision arithmetic, they may differ considerably in practice owing to finite word length effects of roundoff and truncation.

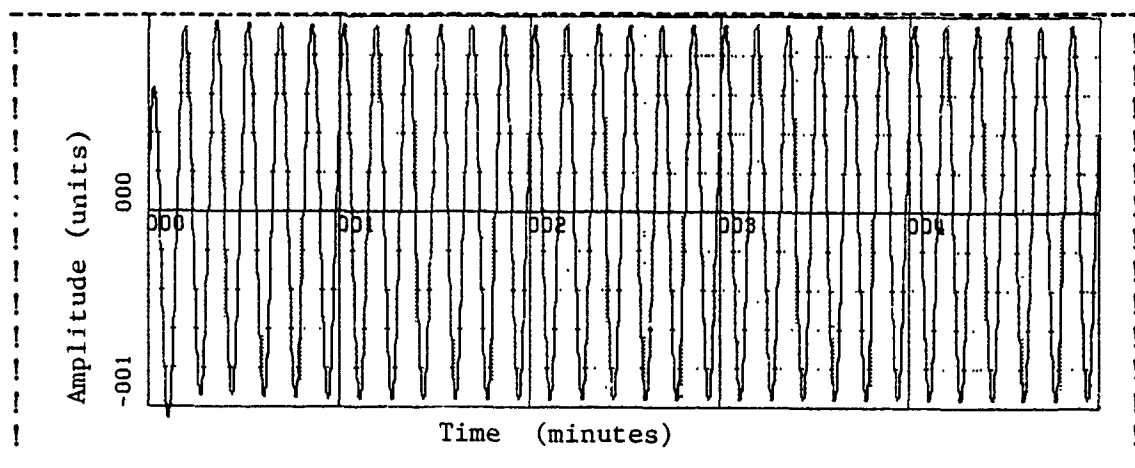


Figure 5.1: Output of First Stage Filter of Digital Filter Computer Program With Sinusoidal Input in Simulation.

Unfortunately, the second stage output of the filter showed an instability within the program design, indicated by the output of the filter being a sinusoid of increasing magnitude, as indicated in Figure 5.2 below.

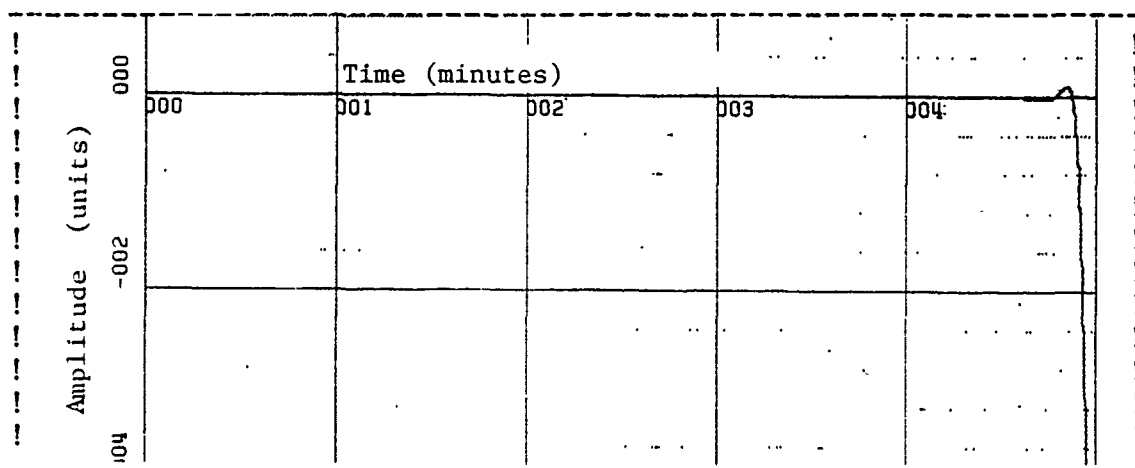


Figure 5.2: Output of Second Stage Filter Design With Input of a Sinusoid.

The stability of the third stage of the filter design was investigated by inputting the sinusoid directly to the third filter, and found to be stable. A check of the derivation of the equations, coefficients, and programming steps of the second (unstable) filter of the design failed to indicate the cause of the instability.

Computation of the poles of the z transfer function, $H(z)$, of the second stage of the filter confirmed the instability of the design. The poles were computed to be: $0.92 \pm 0.1218i$, $1.07 \pm 0.1340i$, 0.8611 , and 1.1564 . Of these six poles, three lie outside the region of convergence for the z -plane, that is, within the unit circle discussed previously in Chapter IV.

The second stage of the filter was therefore redesigned using the cascade form of the direct form realization (direct form II), and tested in simulation. A copy of the software used in the simulation is enclosed in Appendix F.

The output of all three filter stages of the program were stable, as indicated in Figures 5.3 through 5.7 below. The amplitude decrease and phase shift expected were observed. The "damped overshoot" of the second stage output is due to the fact that, for values of the input function prior to time zero in the simulation, utilized in the input-output signal difference equations for the filter, the input signal was set at 0. This resulted in an instantaneous

change of the input signal from 0 to the finite value introduced in the simulation at time 0+. The "overshoot" of the filter is the filter's attempt to "match" this instantaneous jump in magnitude of the input signal. When the input signal to the filter in the simulation is zero at time zero, this overshoot effect does not occur.

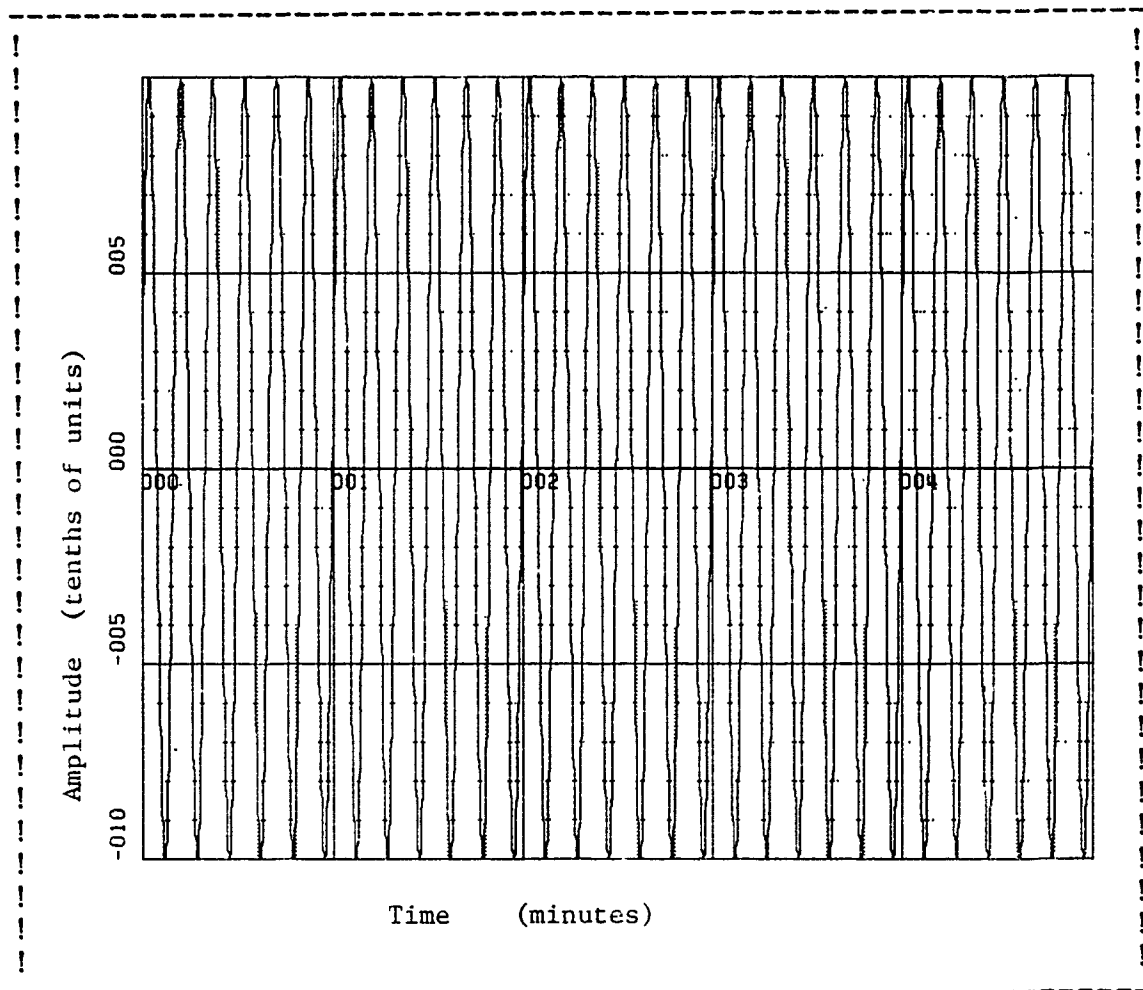


Figure 5.3: Input Signal to Digital Filter Program. A Sinusoid of Frequency 0.1 HZ and Amplitude ± 1 .

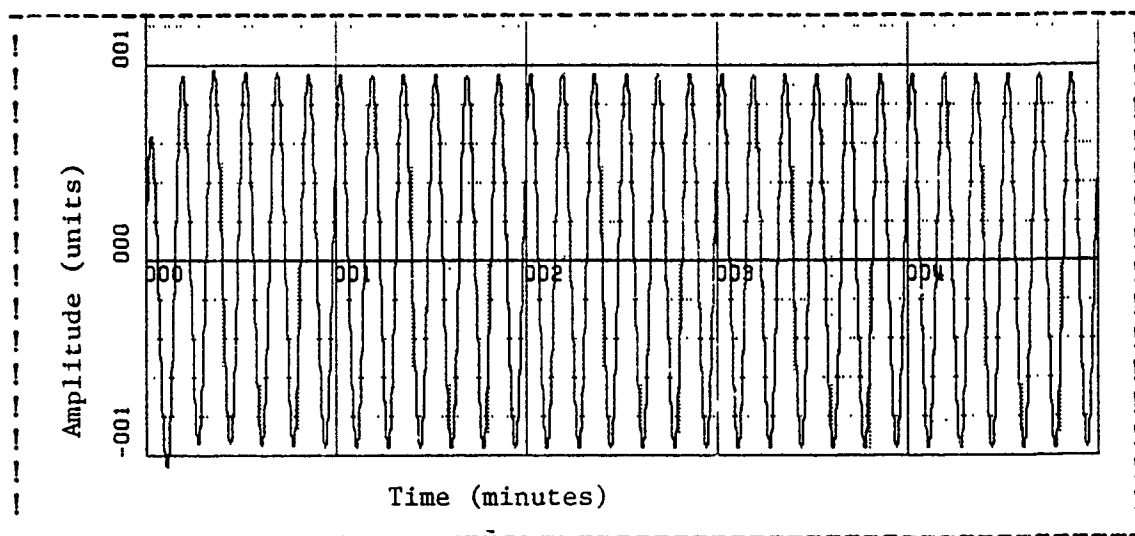


Figure 5.4: Output of First Stage of Digital Filter Program.

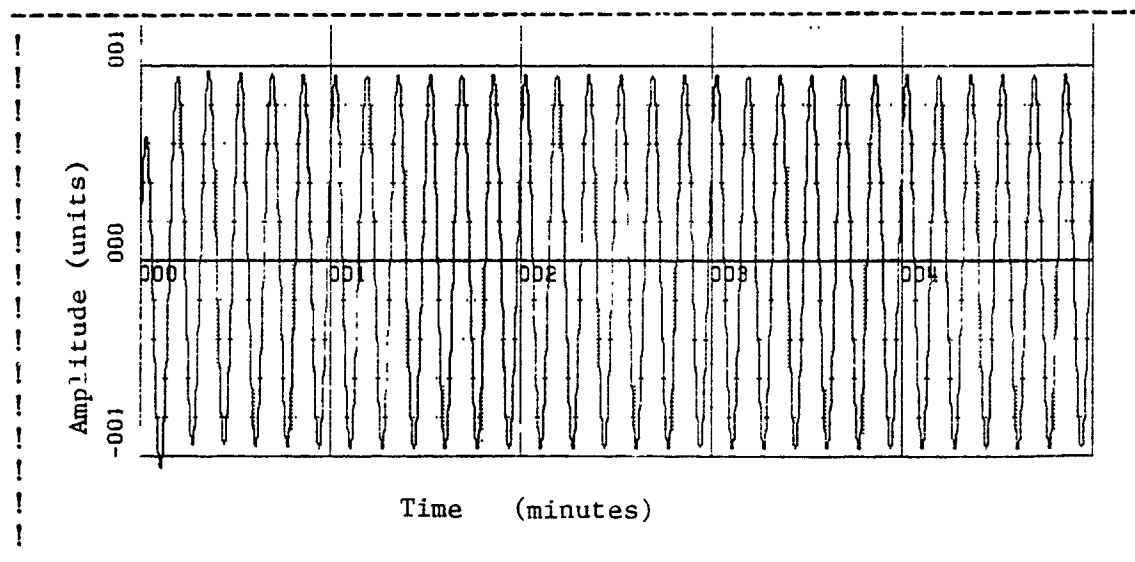


Figure 5.5: Output of Second Stage of Digital Filter Program.

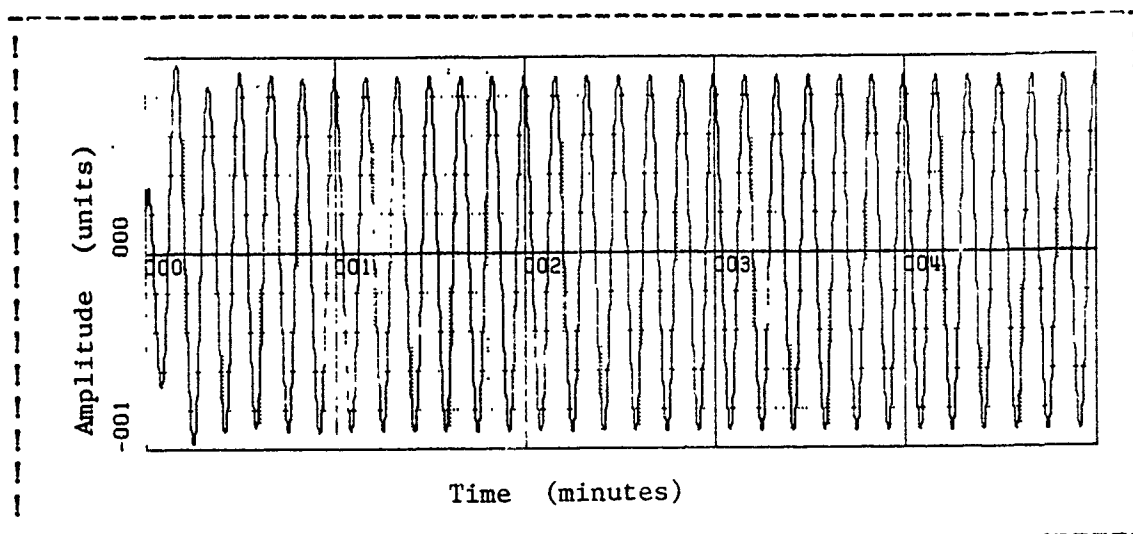


Figure 5.6: Output of Third Stage of Digital Filter Program.

This simulation was run with inputs of sinusoids of various frequencies in order to check the stability of the filter design at frequencies throughout the operating range of the AN/ASQ-81 magnetometer. In all cases, the design was stable, and the expected amplitude changes and phase shifts occurred.

2. Noiselike Inputs

The simulation was also run with inputs consisting of a sinusoid of a frequency which should be passed through the AN/ASQ-81 added to sinusoids of frequencies which should have been filtered by the magnetometer and random noise. The filter performed as expected, with the sinusoid of a passable frequency passed by the filter, and spurious noise and sinusoids attenuated severely. The results of a simulation consisting of a sinusoid of passable frequency, a

filterable sinusoid, and uniformly distributed random noise, all of amplitude ± 1 , are presented in Figures 5.7 through 5.10 below.

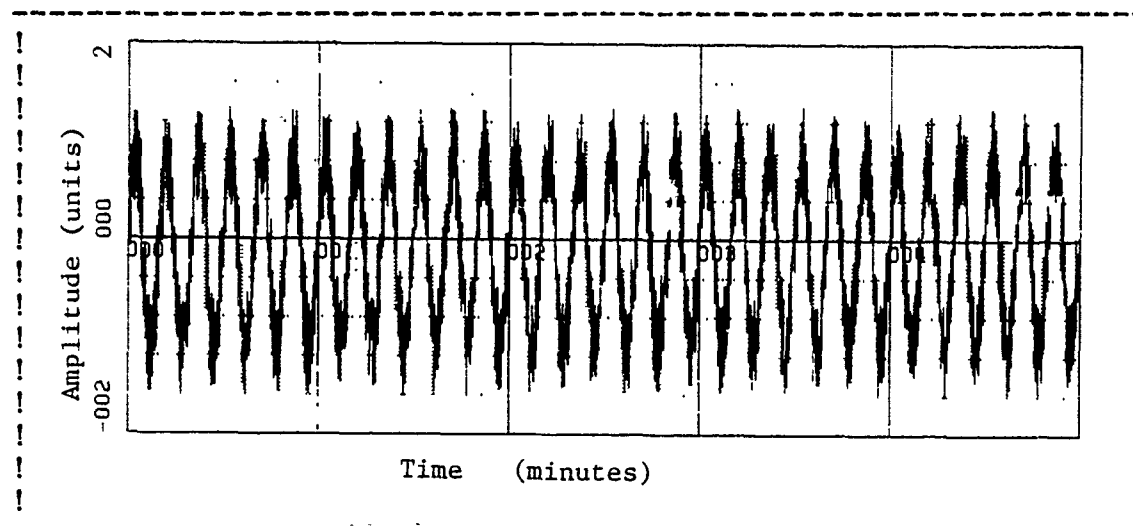


Figure 5.7: Input to Filter - 0.1 HZ Sinusoid, 10 HZ Sinusoid, Uniformly Distributed Random Noise of Amplitude ± 1 .

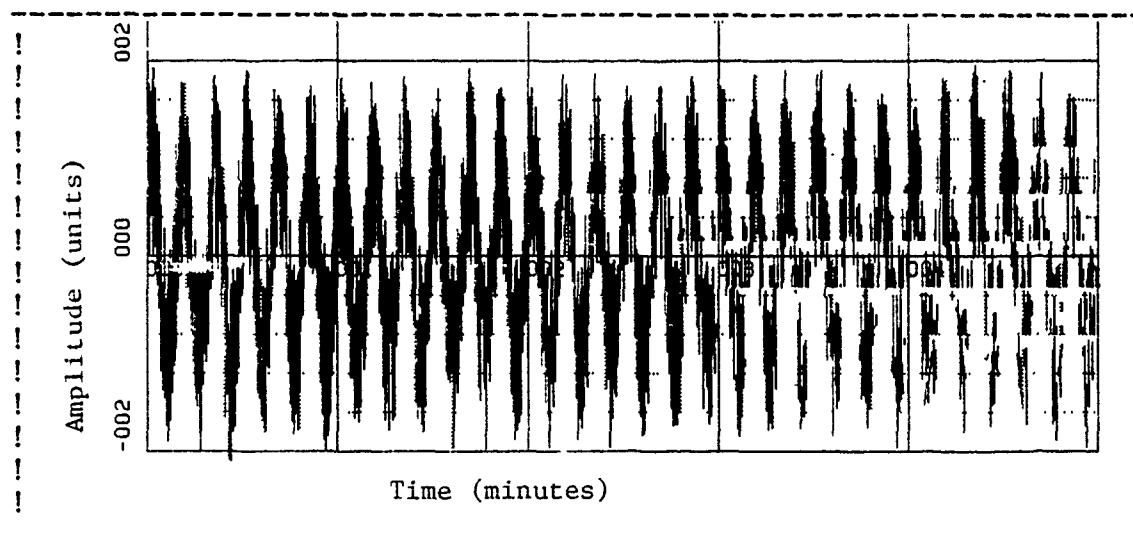


Figure 5.8: Output of First Filter Stage.

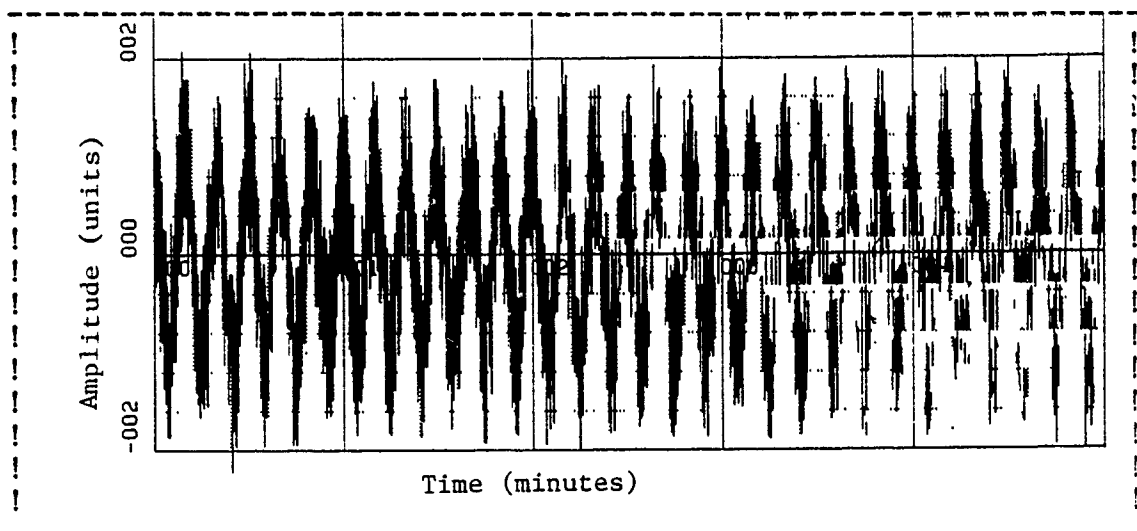


Figure 5.9: Output of Second Filter Stage.

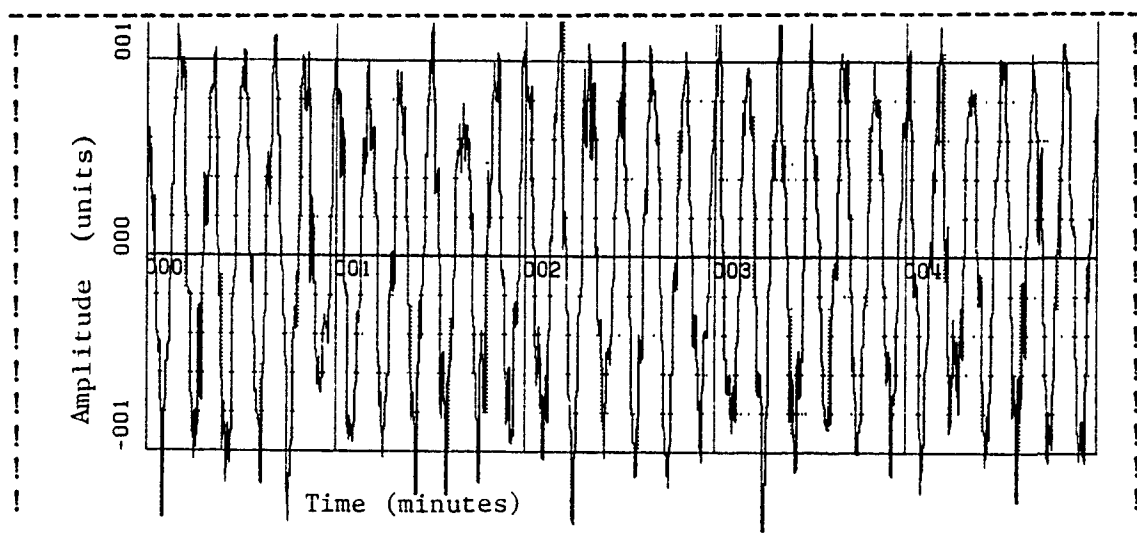


Figure 5.10: Final Filter Stage Output.

As can be seen, the digital filter program succeeds in filtering out random noise and signals of frequency components above the band pass of the magnetometer.

In order to ensure that the digital filter representation of the magnetometer has the same amplitude

versus frequency characteristics of the AN/ASQ-81 magnetometer, a simulation program was written which inputs sinusoids of varying frequencies and computes the Root Mean Square (RMS) value of the filter output and the signal input, then computes the decibel (dB) attenuation of the filter at that frequency. A copy of this program is included in Appendix G. A plot was made of the dB attenuation versus frequency for the filter and compared

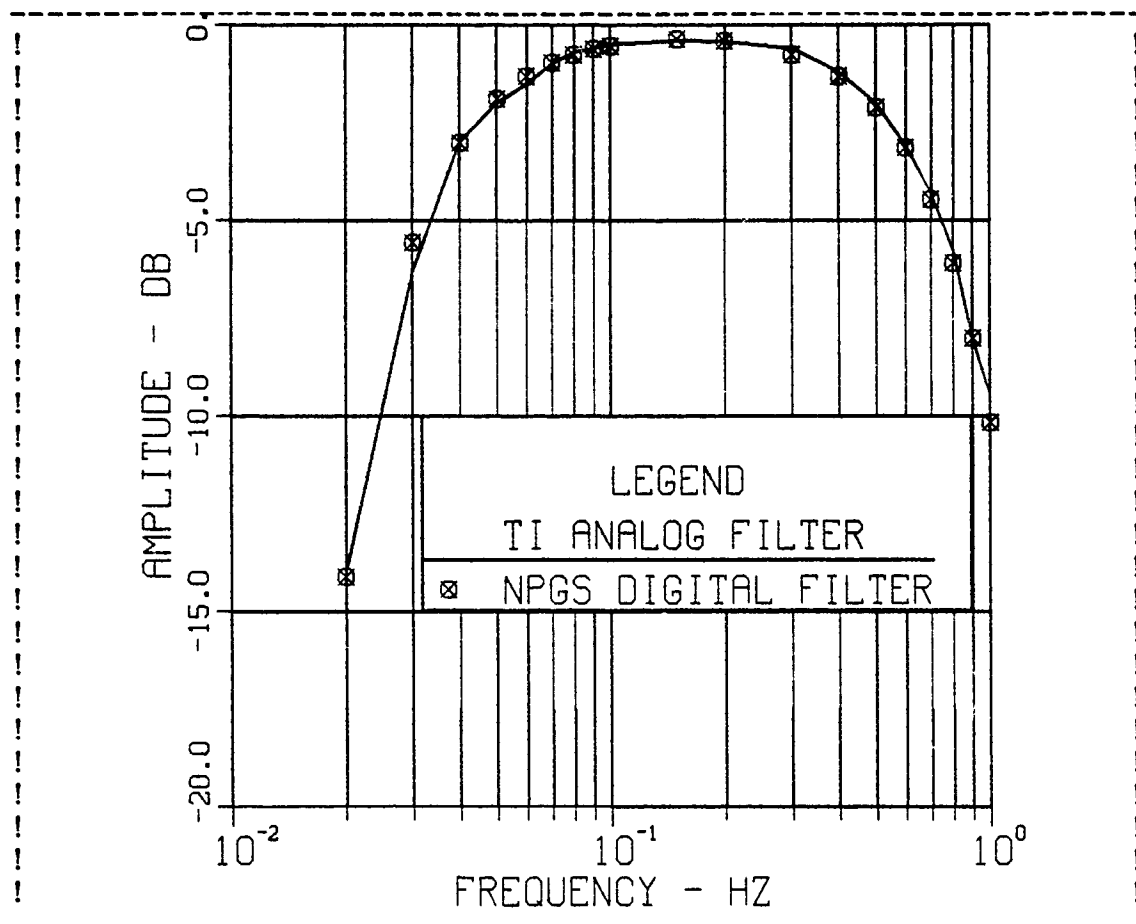


Figure 5.11: Plot of Attenuation Versus Frequency for Sinusoidal Inputs for Digital Filter and Analog Filter.

with the measured frequency performance of the AN/ASQ-81 magnetometer, which was supplied by Texas Instruments, Inc., and does not include the effects of the fixed high pass filter. Consequently, the data shown in Figure 5.11 is a comparison of the data supplied by Texas Instruments and the output of the test program, which also does not include the fixed high pass filter. As can be seen, the performance of the filter is extremely similar to that of the magnetometer itself.

3. Anderson Function Simulations

The next step in the simulation phase was the introduction to the filter of Anderson function simulations. The shape of the signal amplitude of the output of a magnetometer passing through the sphere of influence of a magnetic anomaly (submarine) is a function of the dip angle of the geomagnetic field, the magnetic heading of the track of the magnetometer (or the aircraft), the magnetic heading of the anomaly (submarine) dipole, and the lateral range between the magnetometer (aircraft) and the anomaly. Anderson functions [Ref. 9] are mathematical representations of three basic components of signals which, when taken in various linear combinations, describe the shape of these anomaly signals. The equations for the Anderson functions are:

$$\begin{aligned}
 \text{(First Anderson Function)} \quad f_0 &= \frac{1}{(1 + B)^{2.5/2}} \\
 \text{where} \quad B &= \frac{(\text{velocity}) \times (\text{time})}{\text{range at CPA}},
 \end{aligned}$$

or, a dimensionless parameter defined as the distance traveled along the magnetometer (aircraft) track divided by the slant range at closestpoint of approach (CPA)

$$\begin{aligned}
 \text{(Second Anderson Function)} \quad f_1 &= B \times f_0 \\
 \text{(Third Anderson Function)} \quad f_2 &= B \times f_1^2 = B^3 \times f_0^2
 \end{aligned}$$

The Anderson functions were introduced into the filter program in a noise-free signal environment in order to observe the output signal and ensure that it was a "MAD-like" signal. A rigorous determination of the actual output signal would have been extremely difficult to obtain, so a comparison was made with the output of a computer simulation program provided to NPS by Mr. Joe Rice of Texas Instruments. When the sampling rate of the program was adjusted to equal that of the Texas Instruments program, 8 HZ, the two program outputs were observed to be very similar. The Anderson function simulation inputs and outputs of the program are depicted in Figures 5.12 through 5.18. The Texas Instruments program outputs were obtained in the form of time series plots of discontinuous data points, and were therefore not conducive to replotting for comparison.

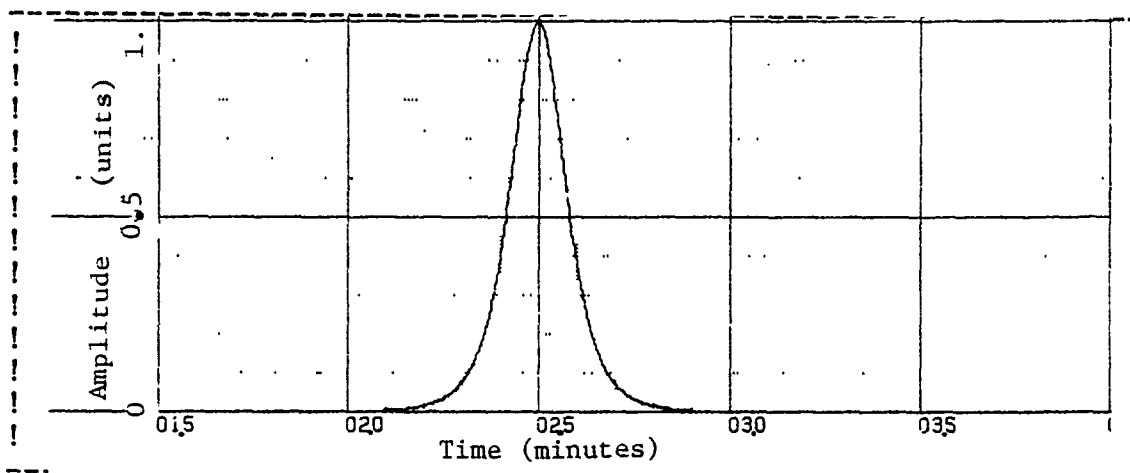


Figure 5.12: First Anderson Function Input. CPA at Time 2.5 Minutes.

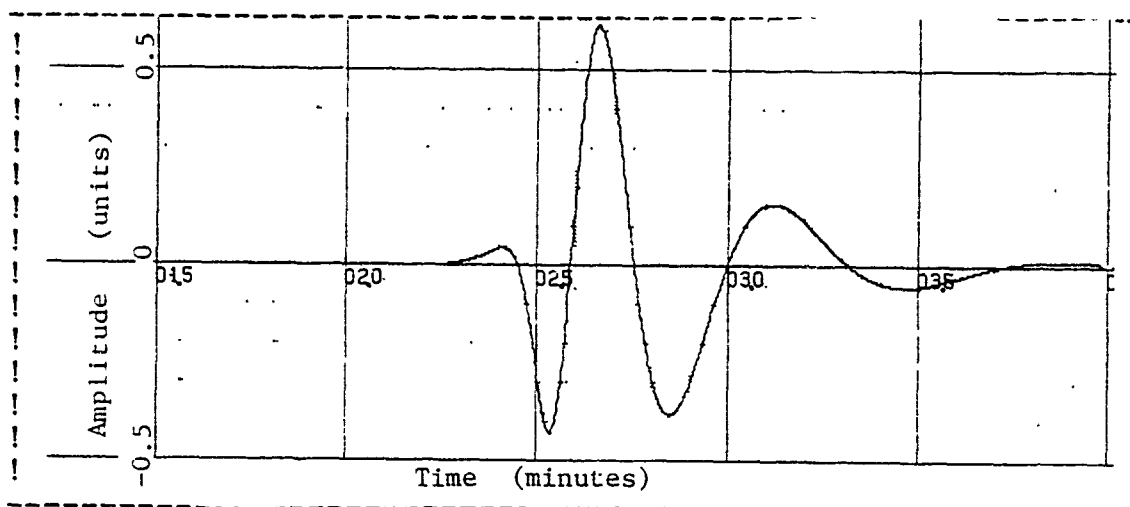


Figure 5.13: Filter Output for First Anderson Function Input.

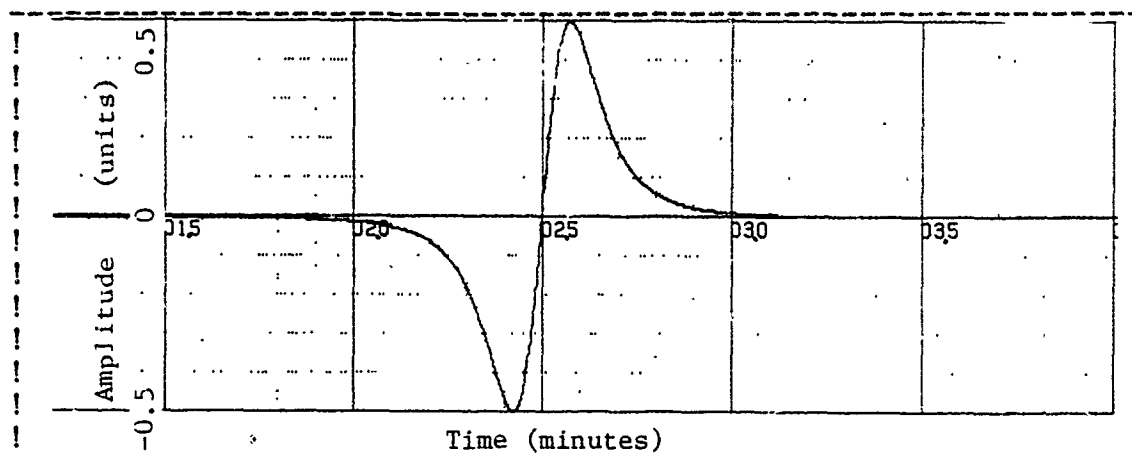


Figure 5.14: Second Anderson Function Input. CPA at Time 2.5 Minutes.

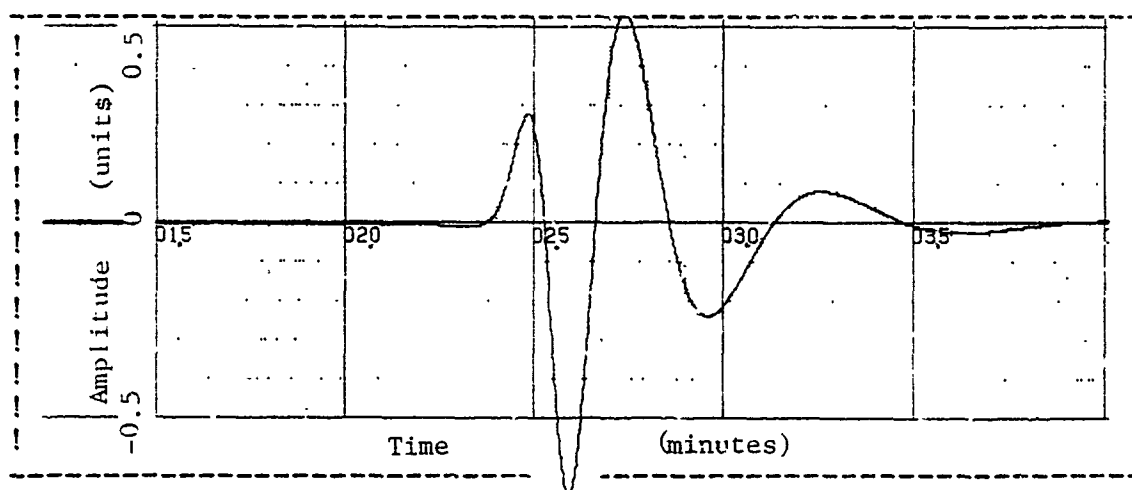


Figure 5.15: Filter Output for Second Anderson Function.

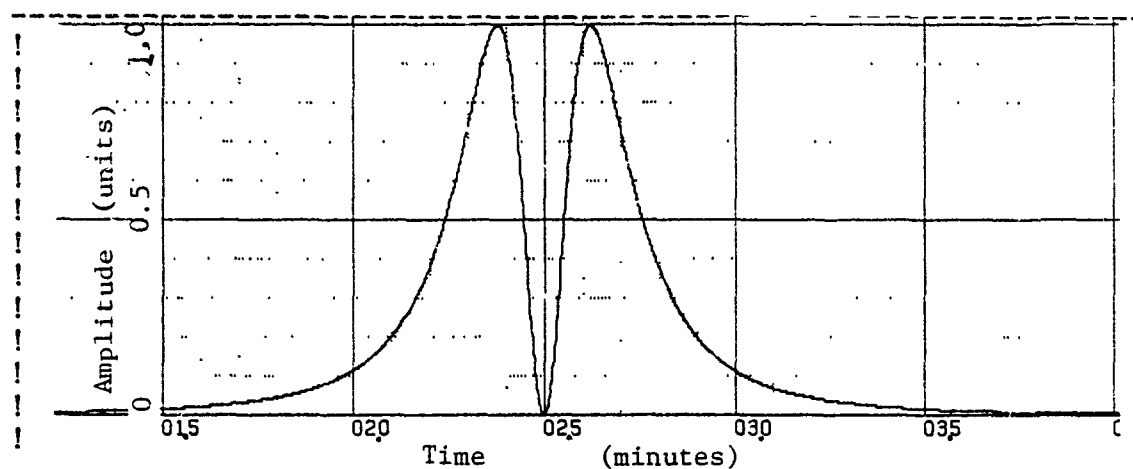


Figure 5.16: Third Anderson Function Input. CPA at Time 2.5 Minutes.

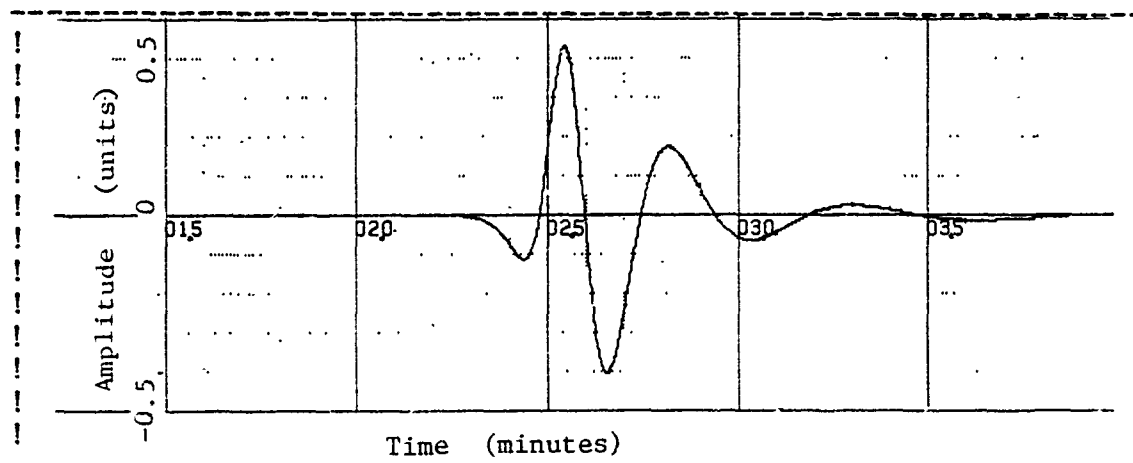


Figure 5.17: Filter Output for Third Anderson Function.

The filter output for all three Anderson function inputs did appear to be "MAD-like" signals, and did closely resemble the simulation output obtained from Texas Instruments, Inc.

4. Impulse Function Response

The response of the filter program was also observed when the input was a unit impulse function. Again, the

output was compared to that of the Texas Instruments' computer program. The outputs of the two programs were observed to be, again, very similar, as can be seen in Figure 5.18, where the response of the NPGS filter is represented by a solid line and that of the Texas Instruments filter by a chain-dash line. The abrupt "jumps" in

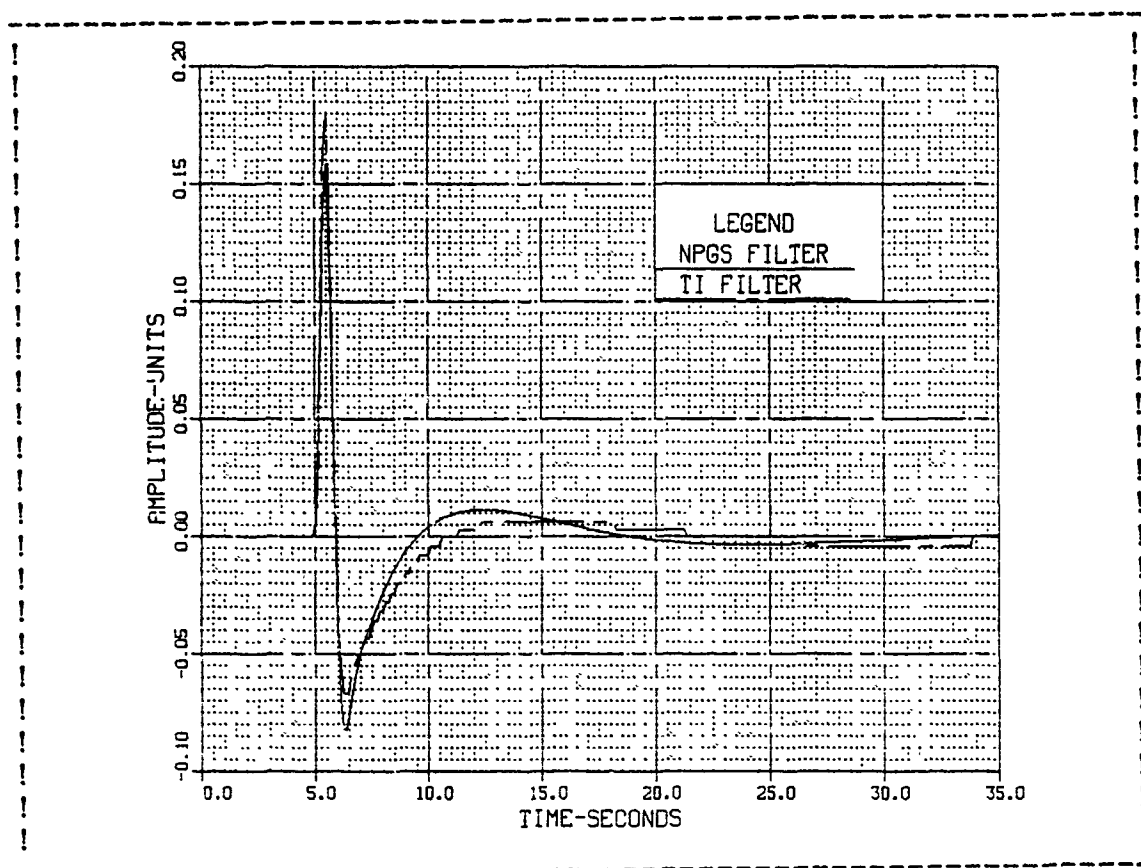


Figure 5.18: Impulse Response of Filters.

of the Texas Instruments response are due to the translation of the output plot supplied to this plot. The plot supplied by Texas Instruments was, again, discontinuous points of poor resolution, and it was necessary to interpolate values

in order to generate Figure 5.18. This resulted in the broken appearance of the plot. Even so, the similarity of the outputs can be observed.

B. EQUIPMENT SETUP

Following the simulation phase of the experiment, actual magnetic field measurements were introduced to the filter in order to test the response of the filter. Magnetic field measurements were made at the La Mesa field test site near the Naval Postgraduate School in Monterey. The output of an AN/ASQ-81 magnetometer, a Schonstedt magnetic field sensor, and the school's coil sensor, oriented along the Earth's magnetic field, were pulse code modulated (PCM) and transmitted via VHF radio to recording devices at the Postgraduate school. The recording of a two hour long data collection period was transferred to digital data tape for use by the school's IBM3033 general purpose mainframe computer.

In the first test of the digital filter program, the output of the Schonstedt sensor, which represents fluctuations of the Earth's total field, was used as the input to the computer program. A comparison of the output of the computer program, with this approximation to the total field fluctuations as input, to the output of the AN/ASQ-81 should provide an indication of the proper functioning of the computer filter program. The results of

the test are shown in Figures 5.19 through 5.21 on the pages following. Figure 5.19, the Schonstedt sensor output, shows several instances of PCM dropouts, that is, occasions where the pulse code modulation signal was not correctly read by the computer for some reason. At such occurrences, the data point value used by the computer is a random number and does not reflect the true value of the data. The problem with these PCM dropouts is that the computer does not recognize them as invalid data points and will use them in computations. This can (and does) cause problems in the computation of Fourier transforms, spectral characteristics, etc. Additionally, this will also impact the proper functioning of the digital filter program which is the subject of this thesis. PCM dropouts are visible at times 6, 8, 142, and 220 through 226 seconds on the plot of the Schonstedt sensor output. An examination of Figure 5.20, the filter program output, reveals the programs attempt to "follow" these PCM dropouts. It should be recalled that previous simulations indicated the filter's tendency to "follow" sudden changes in the input signal, with a relaxation time required for the filter to steady out. This effect is apparent in the output of the filter program at times corresponding to those of the PCM dropouts in the Schonstedt sensor's time series plot. It can be seen that this overshoot tendency resulted in an output significantly different from the actual AN/ASQ-81 output at these times.

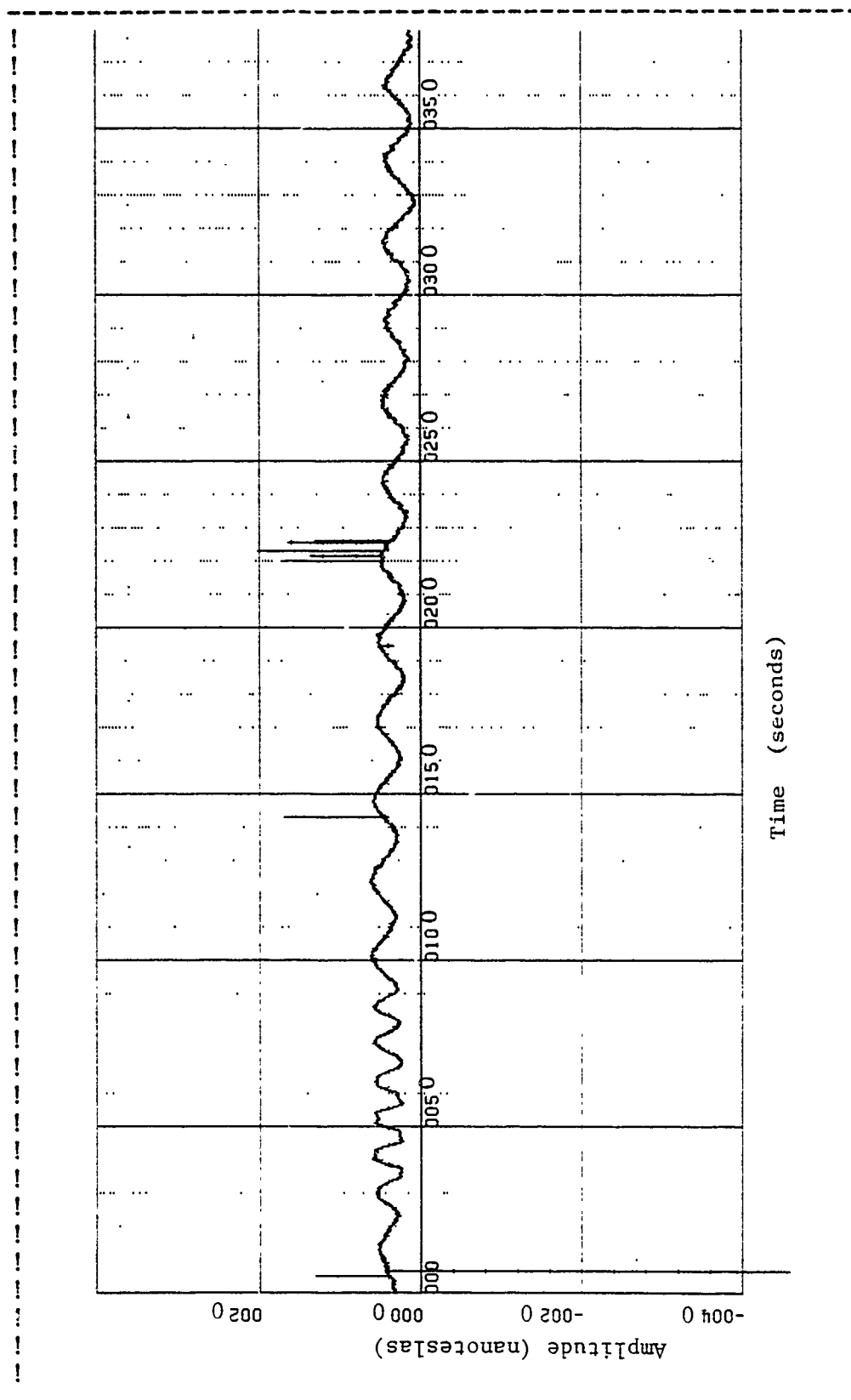


Figure 5.19: Schonstedt Coil Time Series Output

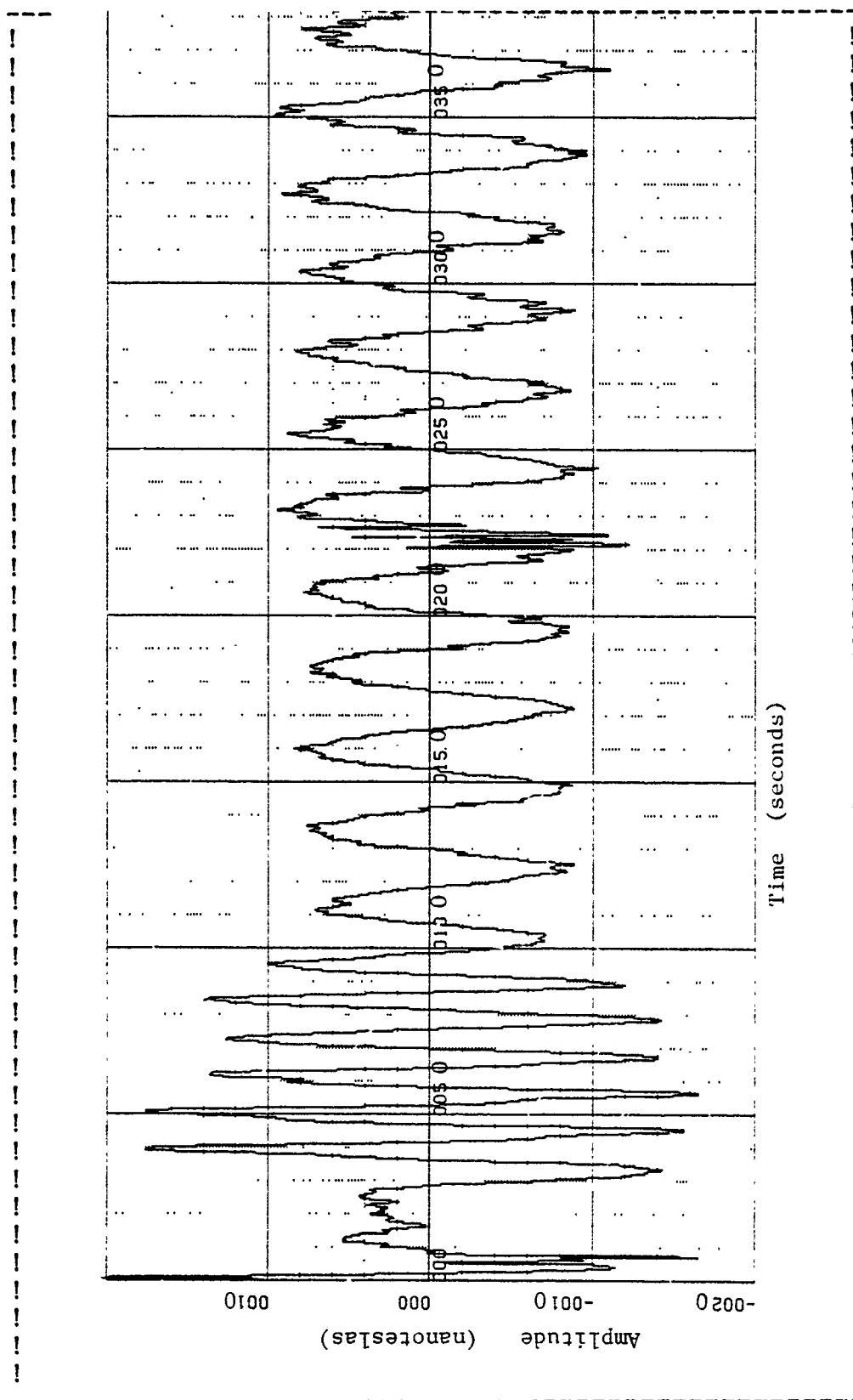


Figure 5.20: Program Time Series Output With Schonstedt Coil as Input

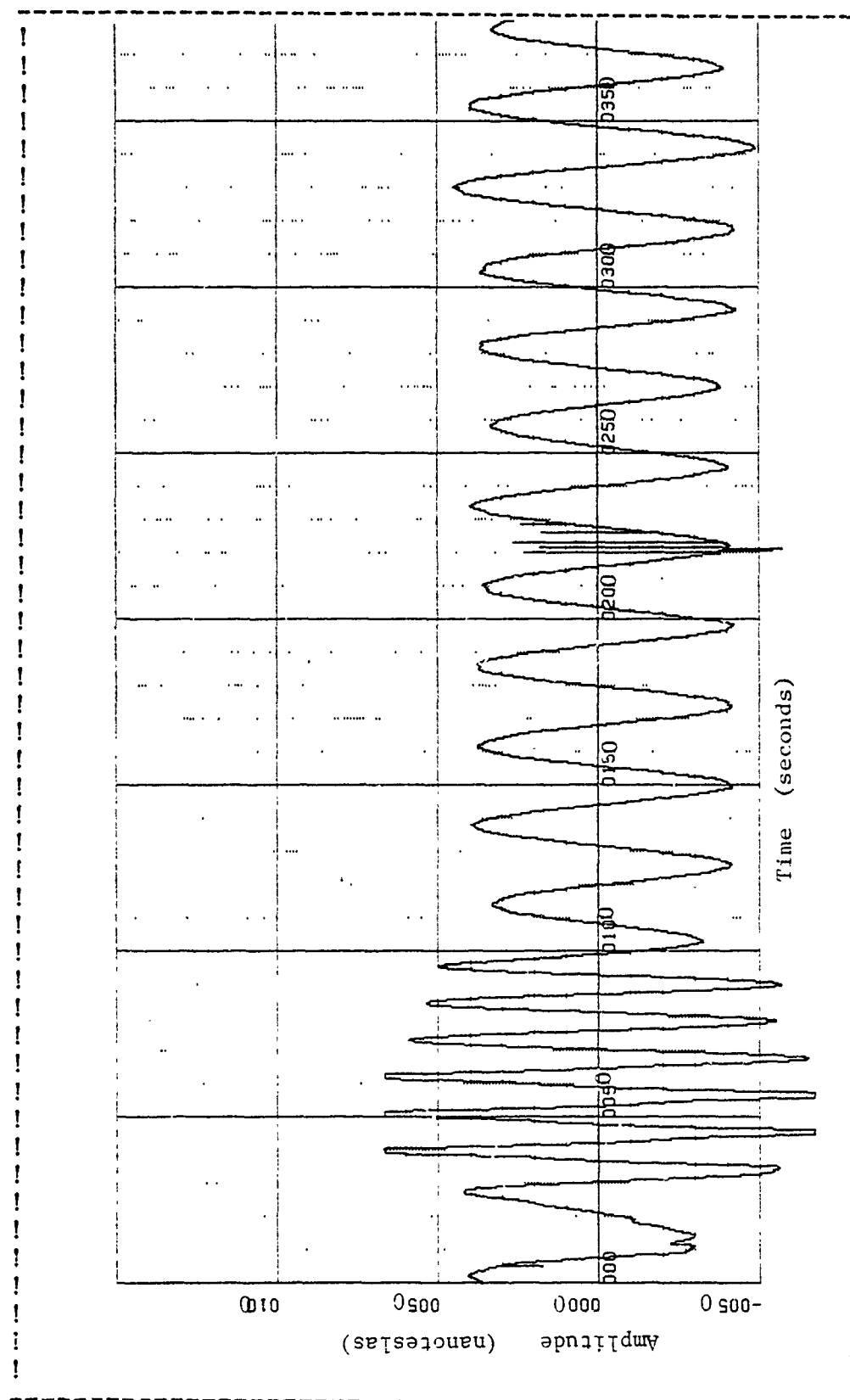


Figure 5.21: ASQ-81 Time Series Output

If the PCM dropout induced differences are neglected, it can be seen that the shape of the output of the filter program is remarkably similar to that of the AN/ASQ-81 magnetometer, although noisier. Note that the output of the AN/ASQ-81 magnetometer exceeded the maximum voltage amplitude which the pre-amplifiers of the data collection system were able to handle and resulted in a truncated signal from time 40 to time 60 seconds. It can still be seen, however, that the filter program output is very similar to the time signal which would have been displayed without this truncation.

It should be noted that the amplitudes of the time series signals of the program output and the AN/ASQ-81 magnetometer differ considerably. In the case of the program output, the peak amplitudes are on the order of 1.4 nanoteslas along the vertical scale, while the peak amplitudes of the output of the AN/ASQ-81 magnetometer are on the order of 0.7 nanoteslas along the vertical scale. This is because the input signal to the filter program is an approximation to the total field difference time series signal, and some amplitude difference could reasonably be expected. The intent of this initial test was to investigate the output time series shape, and an exact correlation was not expected. It is worth noting that the digital filter program will perform its function on any time series signal, regardless of units. This means that a signal may be

operated upon either before or after conversion from whatever units it was originally measured to magnetic field strength units.

Therefore it appears that the digital filter program is functioning properly. When a close approximation to the fluctuations of the total field time series signal is used as the input to the computer program, the output of the program is similar to the time series output of an AN/ASQ-81 magnetometer.

The final stage in the testing process was a conversion of the time series output voltage signal of the coil antenna sensor, which was aligned along the Earth's magnetic field, into a total field fluctuation time series representation for the same time period as before, and then to use this as the input to the digital filter program. A comparison of the resultant time series output of the program with the actual AN/ASQ-81 magnetometer output would validate the proper functioning of the program.

Conversion of the time series antenna sensor output voltage signal into total field fluctuations in nanoteslas was accomplished through the use of a computer program designed by Capt. Kurt Stevens, USAF, a student at the Naval Postgraduate School, as his Master's thesis [Ref 10]. The output voltage time series is stored in an array, then a Fourier transform is performed on the stored data, resulting in the Fourier spectrum of the data. This spectrum is

corrected for the characteristics of the coil antenna sensor to obtain the Fourier spectrum of the total field data. A reverse Fourier transform gives the time series signal for total magnetic field in nanoteslas.

This time series signal was used as the input to the digital filter program and compared with the output of the AN/ASQ-81 magnetometer. Figures 5.22 through 5.24 show the raw coil antenna data, the total field time series data, and the program output time series for a 6 minute period of the test. Figure 5.22 shows the raw coil antenna data series. The number of PCM dropouts should be noted, as these will influence the performance of the filter program. Figure 5.23 shows the computed total field time series. Note that the PCM dropouts evident on the raw time series plot are evident on the computed total field time series plot also, and thus inputted to the filter program as valid data points. Additionally, there are two "jumps" in the plot of total field fluctuation (Figure 5.23) which are also inputted to the filter program as valid data points. These "jumps" are located at 128 and 256 seconds and are caused by the method of processing blocks of data for the conversion to total field fluctuation. A block of 128 seconds of data is processed at a time, and the results of each block are stored in an array. This results in a slight amplitude difference between the last data point of one block and the

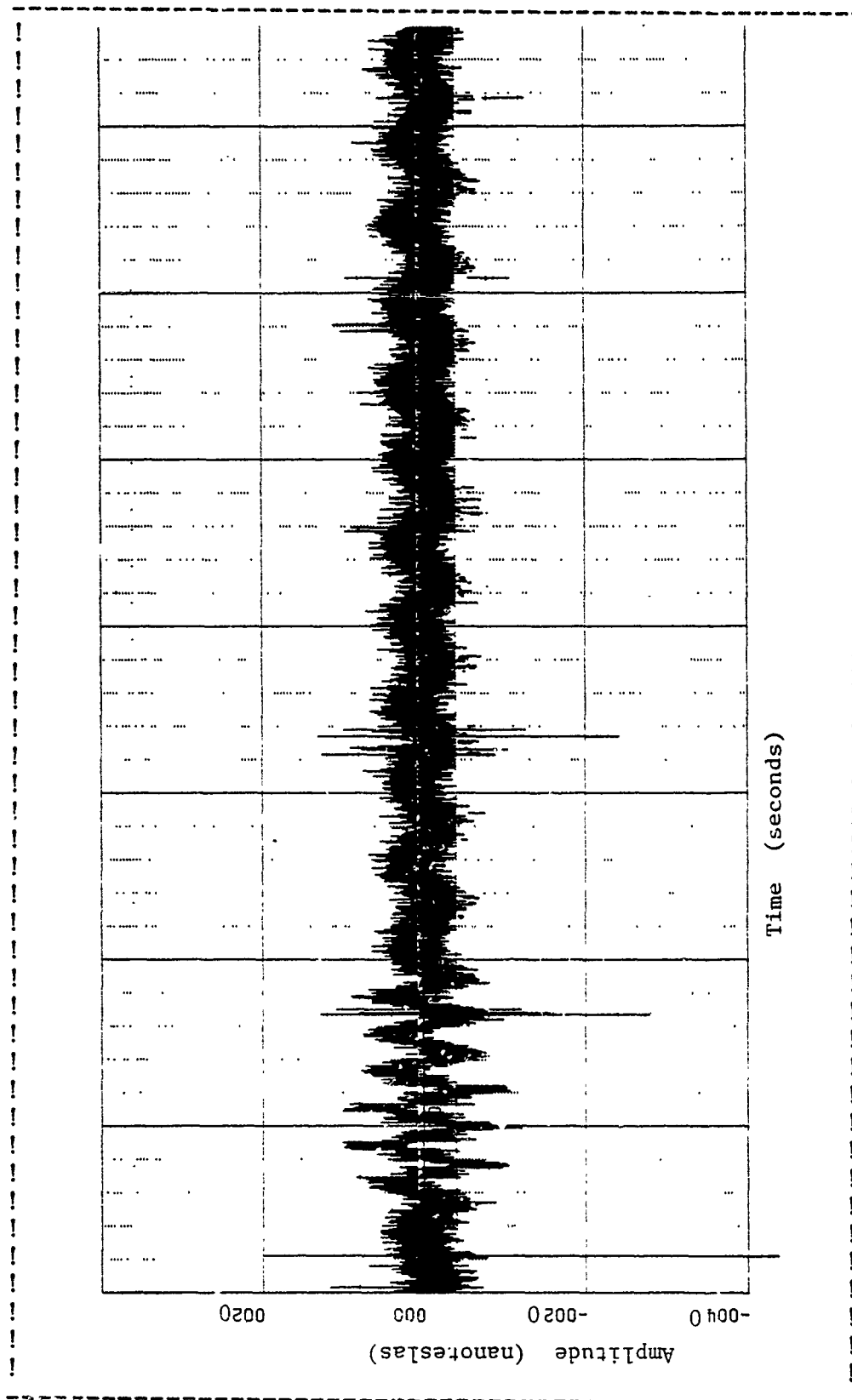


Figure 5.22: Raw Coil Antenna Time Series Output

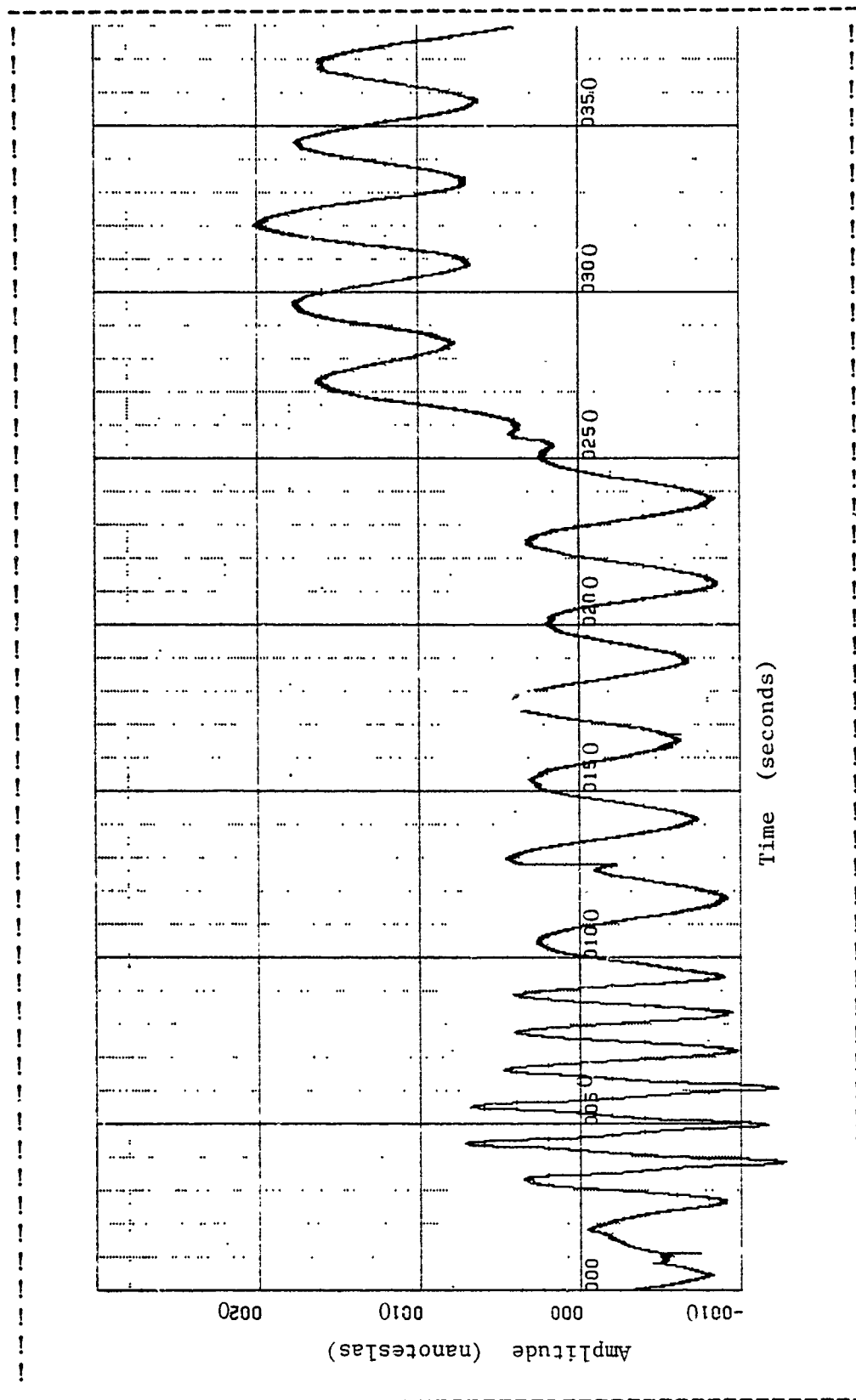


Figure 5.23: Coil Antenna Difference Field Time Series Output

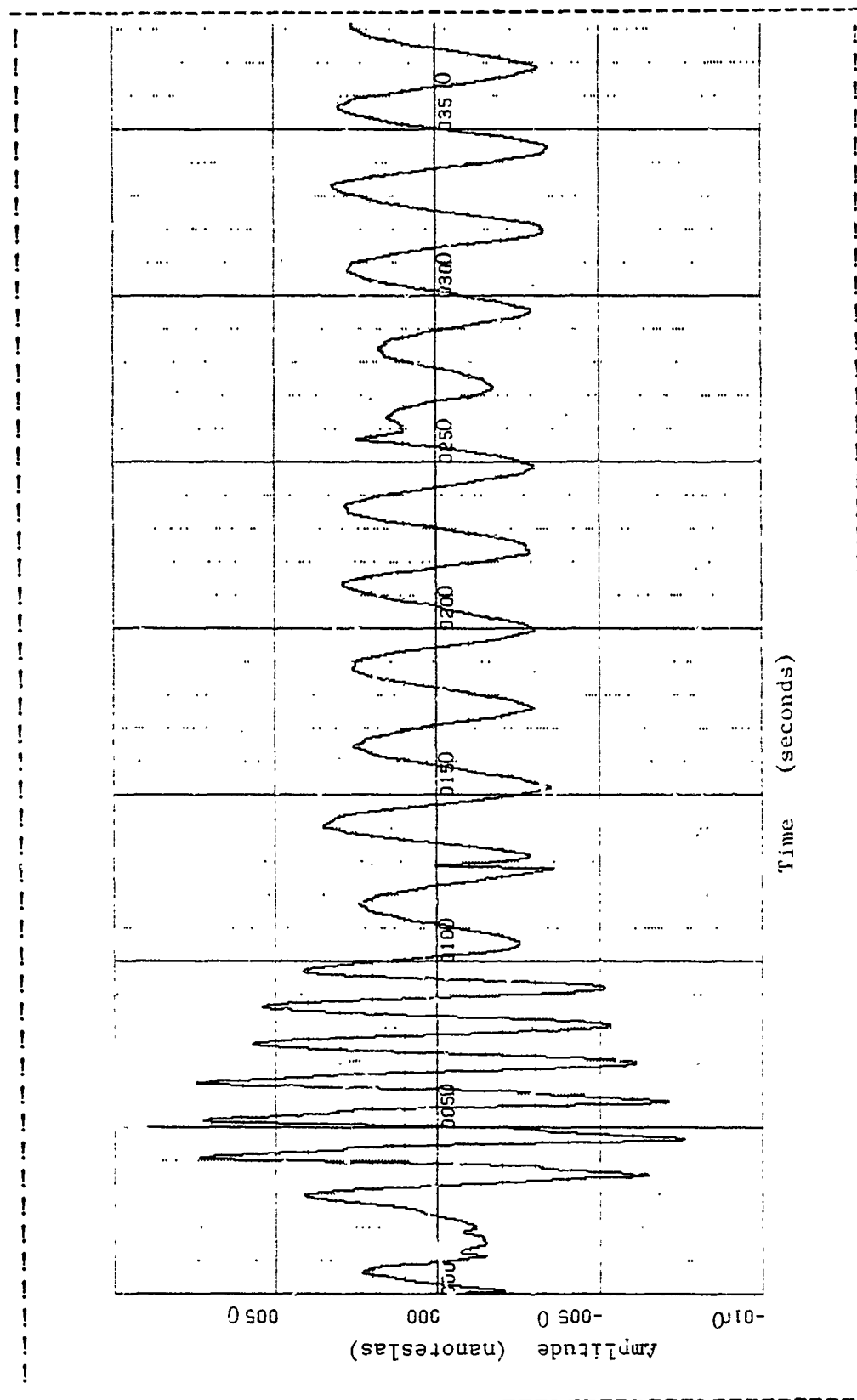


Figure 5.24: Program Time Series Output With Coil Antenna Difference Field Time Series as Input.

first data point of the next block of data. This slight difference is manifested as a signal jump.

A comparison of Figures 5.24 (program output) and 5.21 (AN/ASQ-81 output) show that the filter program gives a time series output very similar to that of the actual magnetometer. The first 20 seconds of the program output is somewhat dissimilar to that of the AN/ASQ-81, due either to the initial "start up" delay of the filter program or to distortion of the total field fluctuation time series. There is a PCM dropout at time 11 seconds which contributed to the distortion.

Following this, however, it can be seen that the program output is very similar to that of the magnetometer, except at 128 and 256 seconds, which show the effects of the false signal jumps caused by the total field fluctuation conversion. There is also a noticeable four to five second time delay between the AN/ASQ-81 output and that of the filter program. As this delay is not evident in a comparison of the AN/ASQ-81 output and that of the filter program with the Schonstedt sensor as the input, it can be inferred that this time delay is caused either by the program which converts the raw coil data to total field fluctuation data, or by a phase (and hence time) change of the voltage signal due to the coil sensor itself. A comparison of the raw coil data in Figure 5.22 to the converted coil data in Figure 5.23 indicates no time shift,

and hence the deduction can be made that there is a time delay inherent within the coil sensor itself.

Other than the differences of the four to five second time delay and the distortions caused by the false signal jumps, the program output is extremely similar to the output of the AN/ASQ-81 magnetometer.

VI. CONCLUSIONS

The intent of this thesis was to design and test a digital filter computer program which would, when given a time series input of fluctuations in the total magnetic field, deliver an output time series representation of the output of an AN/ASQ-81 magnetometer. This purpose has been realized.

The computer program contained in Appendix I has been proven to output a time series signal which is very similar to that of the magnetometer. The major limitations of the output signal are a finite time delay of about five seconds between the AN/ASQ-81 magnetometer signal and the output signal of the program, a sensitivity of the program to false data points such as those caused by PCM dropouts and false signal jumps caused by processing large data blocks, and the inherent limitations of the program caused by its dependence on the use of digital data tapes and the IBM 3033 mainframe computer.

The five second time delay is not considered to be an important limitation to the program, as it was intended as a research tool for programs currently in progress at the Naval Postgraduate School. Instances where this time delay might become important would be in areas of simultaneous comparison of the program output signal with an actual magnetometer, in target location algorithms using time

delays, or in correlation studies between different sensors. In correlation studies using coil sensors, the effects of the time delay would cancel out, as all coil outputs would be similarly delayed. In target location algorithms, the target location errors due to the time delay could be adjusted for simply while in computer simulation, and flight testing could not reasonably be accomplished without the use of an actual magnetometer as the sensor. Lastly, in a comparison of the program output with an actual sensor, the time delay can, again, be compensated for. In short, these limitations are not considered excessive, especially as the apparent cause for the delay is not the filter program.

In the primarily intended purpose of the filter program, magnetic noise studies, the time delay is not considered to be a problem.

The problem of false data points caused by PCM dropouts and signal jumps due to conversion to total field fluctuations is more serious. False data points cause inaccuracies in the output time series and could adversely affect later projects. Unfortunately the PCM dropout problem is one which is endemic to the data collection system presently being used at the postgraduate school, and not to the filter program itself. It is imperative that users of this program are aware of the PCM dropout problem and of the effects it may entail upon their specific

research. A large number of PCM dropouts in a time series could render that series unusable. Similarly the case of the false data jumps caused by conversion to total field fluctuations is not within the filter program. Further investigation of this problem is necessary in order to eliminate it.

The last problem, that of reliance upon the digital data tape/IBM 3033 computer system, is, like the PCM problem, one which is not endemic to the filter program but rather to the data collection system being used. A change of data collection system may, at some future time, remove the reliance upon the PCM/digital tape/IBM 3033 data system (and hence too the data block conversion problem which results in false data jumps), but this is unlikely at this time. Users should be aware of this dependence and of possible effects upon specific research projects.

APPENDIX A

AN/ASQ-81 FILTER TRANSFER FUNCTIONS

Fixed High Pass Transfer Function:

$$H(S) = \frac{80 S^2}{80 S^2 + 20 S + 1}$$

Selectable High Pass Transfer Functions:

A. 0.04 HZ

$$H(S) = \frac{40.82834 S^2}{40.82834 S^2 + 12.52096 S + 1} \times \frac{45.28317 S^2}{45.28317 S^2 + 11.00999 S + 1} \times \frac{57.576688 S^2}{57.576688 S^2 + 7.41498 S + 1}$$

B. 0.06 HZ

$$H(S) = \frac{18.14591 S^2}{18.14591 S^2 + 8.34727 S + 1} \times \frac{20.12587 S^2}{20.12587 S^2 + 7.33999 S + 1} \times \frac{25.58964 S^2}{25.58964 S^2 + 4.94332 S + 1}$$

C. 0.08 HZ

$$H(S) = \frac{10.20708 S^2}{10.20708 S^2 + 6.26045 S + 1} \times \frac{11.32080 S^2}{11.32080 S^2 + 5.50500 S + 1} \times \frac{14.39417 S^2}{14.39417 S^2 + 3.70749 S + 1}$$

$$\begin{aligned}
 \text{D. } & \underline{0.10 \text{ HZ}} \quad H(S) = \\
 & \frac{6.53253 S^2}{6.53253 S^2 + 5.00836 S + 1} \times \frac{7.24531 S^2}{7.24531 S^2 + 4.40400 S + 1} \\
 & \times \frac{9.21227 S^2}{9.21227 S^2 + 2.96599 S + 1}
 \end{aligned}$$

Selectable Low Pass Transfer Functions

$$\begin{aligned}
 \text{A. } & \underline{0.2 \text{ HZ}} \quad H(S) = \\
 & \frac{1}{0.3143 S^2 + 1.0741 S + 1} \times \frac{1}{0.2501 S^2 + 0.6209 S + 1}
 \end{aligned}$$

$$\begin{aligned}
 \text{B. } & \underline{0.4 \text{ HZ}} \quad H(S) = \\
 & \frac{1}{0.07858 S^2 + 0.53706 S + 1} \times \frac{1}{0.06252 S^2 + 0.31044 S + 1}
 \end{aligned}$$

$$\begin{aligned}
 \text{C. } & \underline{0.6 \text{ HZ}} \quad H(S) = \\
 & \frac{1}{0.03492 S^2 + 0.35804 S + 1} \times \frac{1}{0.02779 S^2 + 0.20696 S + 1}
 \end{aligned}$$

APPENDIX B

AN/ASQ-81 Z TRANSFORM FILTER TRANSFER FUNCTIONS FOR DIRECT FORM I REALIZATION

For fixed high pass filter:

$$H(Z) = \frac{BFHP0 + BFHP1*Z^{-1} + BFHP2*Z^{-2}}{1 - AFHP1*Z^{-1} - AFHP2*Z^{-2}}$$

where BFHP0, BFHP1, BFHP2, AFHP1, AFHP2 are constants tabulated in Appendix D.

For selectable high pass filter:

$$H(Z) = \frac{BSHP0 + BSHP1*Z^{-1} + BSHP2*Z^{-2} + BSHP3*Z^{-3} + BSHP4*Z^{-4} + BSHP5*Z^{-5} + BSHP6*Z^{-6}}{1 - ASHP1*Z^{-1} - ASHP2*Z^{-2} - ASHP3*Z^{-3} - ASHP4*Z^{-4} - ASHP5*Z^{-5} - ASHP6*Z^{-6}}$$

where, for low frequency cutoff of 0.04 HZ:

$$BSHP0 = 0.99471378$$

$$BSHP1 = -5.9682827$$

$$BSHP2 = 14.920707$$

$$BSHP3 = -19.894276$$

$$BSHP4 = 14.920707$$

$$BSHP5 = -5.9682817$$

$$BSHP6 = 0.99471372$$

$$ASHP1 = 5.9894021$$

$$ASHP2 = -14.947051$$

$$ASHP3 = 19.894225$$

$$ASHP4 = -14.894327$$

$$ASHP5 = 5.9472141$$

$$ASHP6 = -0.98945296$$

For low frequency cutoff of 0.06 HZ:

BSHP0 =	0.9920813		
BSHP1 =	-5.9524928	ASHP1 =	5.9841070
BSHP2 =	14.881232	ASHP2 =	-14.920650
BSHP3 =	-19.841643	ASHP3 =	19.841528
BSHP4 =	14.881232	ASHP4 =	-14.841757
BSHP5 =	-5.9524927	ASHP5 =	5.9209919
BSHP6 =	0.99208212	ASHP6 =	-0.98422128

For low frequency cutoff of 0.08 HZ:

BSHP0 =	0.98945806		
BSHP1 =	-5.9367483	ASHP1 =	5.9788144
BSHP2 =	14.841871	ASHP2 =	-14.894276
BSHP3 =	-19.789161	ASHP3 =	19.788959
BSHP4 =	14.841871	ASHP4 =	-14.789365
BSHP5 =	-5.9367476	ASHP5 =	5.8948841
BSHP6 =	0.98945802	ASHP6 =	-0.97901720

For low frequency cutoff of 0.1 HZ:

BSHP0 =	0.98684156		
BSHP1 =	-5.9210493	ASHP1 =	5.9735244
BSHP2 =	14.802623	ASHP2 =	-14.867941
BSHP3 =	-19.736831	ASHP3 =	19.736516
BSHP4 =	14.802623	ASHP4 =	-14.737149
BSHP5 =	-5.9210491	ASHP5 =	5.8688889
BSHP6 =	0.9868415	ASHP6 =	-0.97384065

For selectable low pass filter:

$$H(Z) = \frac{BSLP_0 + BSLP_1 * Z^{-1} + BSLP_2 * Z^{-2} + BSLP_3 * Z^{-3} + BSLP_4 * Z^{-4}}{1 - ASLP_1 * Z^{-1} - ASLP_2 * Z^{-2} - ASLP_3 * Z^{-3} - ASLP_4 * Z^{-4}}$$

where BSLP₀, BSLP₁, BSLP₂, BSLP₃, BSLP₄, ASLP₁, ASLP₂, ASLP₃, ASLP₄ are constants tabulated in Appendix D.

APPENDIX C

AN/ASQ-81 Z TRANSFORM FILTER TRANSFER FUNCTIONS DIRECT FORM II REALIZATION

For fixed high pass filter:

$$H(Z) = \frac{BFHP0 + BFHP1*Z^{-1} + BFHP2*Z^{-2}}{1 - AFHP1*Z^{-1} - AFHP2*Z^{-2}}$$

where BFHP0, BFHP1, BFHP2, AFHP1, AFHP2 are constants tabulated in Appendix D.

For selectable high pass filter:

$$H(Z) = ASHP1 \times \frac{1 - 2*Z^{-1} + Z^{-2}}{1 - ASHP3*Z^{-1} - ASHP2*Z^{-2}} \times \frac{1 - 2*Z^{-1} + Z^{-2}}{1 - ASHP4*Z^{-1} - ASHP5*Z^{-2}} \times \frac{1 - 2*Z^{-1} + Z^{-2}}{1 - ASHP6*Z^{-1} - ASHP7*Z^{-2}}$$

where ASHP1, ASHP2, ASHP3, ASHP4, ASHP5, ASHP6, ASHP7 are constants and tabulated in Appendix D.

For selectable low pass filter:

$$H(Z) = \frac{BSLP0 + BSLP1*Z^{-1} + BSLP2*Z^{-2} + BSLP3*Z^{-3} + BSLP4*Z^{-4}}{1 - ASLP1*Z^{-1} - ASLP2*Z^{-2} - ASLP3*Z^{-3} - ASLP4*Z^{-4}}$$

where BSLP0, BSLP1, BSLP2, BSLP3, BSLP4, ASLP1, ASLP2, ASLP3, ASLP4 are constants tabulated in Appendix D.

APPENDIX D

Z TRANSFORM REALIZATION DIFFERENCE EQUATIONS

With reference to Figures 3.2 and 4.2, the following difference equations are used to model the AN/ASQ-81 magnetometer filter transfer functions. The input to the fixed high pass filter is called SIG(I), where I is the current data sample. The output of the fixed high pass filter, which is the input to the selectable high pass filter, is YO(I), and the output of the selectable high pass filter, the input to the selectable low pass filter, is called YPO(I). The output of the filter is called ASQ(I). (I-1) denotes a time delay of one sample, and so forth, and the symbol * denotes multiplication.

For the fixed high pass filter:

$$YO(I) = BFHP0 * SIG(I) + BFHP1 * SIG(I-1) + BFHP2 * SIG(I-2) + AFHP1 * YO(I-1) + AFHP2 * YO(I-2)$$

where:

$$BFHP0 = 0.9980499222938581$$

$$BFHP1 = -1.9960998445877161 \quad AFHP1 = 1.9960983216843922$$

$$BFHP2 = 0.998049922238581 \quad AFHP2 = -0.9961013674910398$$

For the selectable high pass filters:

$$XI(I) = ASHP1 * YO(I) + ASHP2 * XI(I-2) + ASHP3 * XI(I-3)$$

$$XII(I) = XI(I) + XI(I-2) - 2 * XI(I-1)$$

$$XIII(I) = XII(I) + ASHP4 * XIII(I-1) + ASHP5 * XIII(I-2)$$

$$XIV(I) = XIII(I) - 2 * XIII(I-1) + XIII(I-2)$$

$$XV(I) = XIV(I) + ASHP6 * XV(I-1) + ASHP7 * XV(I-2)$$

$$YPO(I) = XV(I) - 2 * XV(I-1) + XV(I-2)$$

For the low frequency cutoff at 0.04 HZ:

$$ASHP1 = 0.994713789347288 \quad ASHP2 = -0.9952196910157882$$

$$ASHP3 = 1.9952137256322473 \quad ASHP4 = 1.9962028201103847$$

$$ASHP5 = -0.9962082013015601 \quad ASHP6 = 1.9979855321466768$$

$$ASHP7 = -0.9979897681491607$$

For the low frequency cutoff at 0.06 HZ:

$$ASHP1 = 0.9920821277199393 \quad ASHP2 = -0.9928381306174365$$

$$ASHP3 = 1.9928247245317958 \quad ASHP4 = 1.9943056083414792$$

$$ASHP5 = -0.9943177045263504 \quad ASHP6 = 1.9969766455640039$$

$$ASHP7 = -0.9969861717656565$$

For the low frequency cutoff at 0.08 HZ:

$$ASHP1 = 0.9894580558875787 \quad ASHP2 = -0.9904622611337722$$

$$ASHP3 = 1.9904384565912725 \quad ASHP4 = 1.9924092959984783$$

$$ASHP5 = -0.9924307799269113 \quad ASHP6 = 1.9959666590811389$$

$$ASHP7 = -0.9959835860201267$$

For the low frequency cutoff at 0.10 HZ:

$$ASHP1 = 0.9869415560096681 \quad ASHP2 = -0.9880929619779491$$

$$ASHP3 = 1.9880549117849344 \quad ASHP4 = 1.9905139074397893$$

$$ASHP5 = -0.9905474442556225 \quad ASHP6 = 1.9949555824611562$$

$$ASHP7 = -0.9949820174650785$$

For the selectable low pass filters:

$$ASQ(I) = ASLP1 * ASQ(I-1) + ASLP2 * ASQ(I-2) + ASLP3 * ASQ(I-3)$$

$$+ ASLP4 * ASQ(I-4) + BSLP0 * YPO(I) + BSLP1 * YPO(I-1)$$

$$+ BSLP2 * YPO(I-2) + BSLP3 * YPO(I-3) + BSLP4 * YPO(I-4)$$

For the high frequency cutoff at 0.2 KZ:

BSLP0 = 0.0000000452616229

BSLP1 = 0.0000001810464917 ASLP1 = 3.9082436339591027

BSLP2 = 0.0000002715697375 ASLP2 = -5.7285022156249328

BSLP3 = 0.0000001810464917 ASLP3 = 3.7321935213310065

BSLP4 = 0.0000000452616229 ASLP4 = -0.9119356638511430

For the high frequency cutoff at 0.4 HZ:

BSLP0 = 0.0000006918001209

BSLP1 = 0.0000027672004837 ASLP1 = 3.8173771378993420

BSLP2 = 0.0000041508007256 ASLP2 = -5.4670046844062743

BSLP3 = 0.0000027672004837 ASLP3 = 3.4812554457127576

BSLP4 = 0.0000006918001209 ASLP4 = -0.8316389680077603

For the high frequency cutoff at 0.6 HZ:

BSLP0 = 0.0000033463317975

BSLP1 = 0.0000133853271900 ASLP1 = 3.7274299052305002

BSLP2 = 0.0000200779907850 ASLP2 = -5.2152772583906819

BSLP3 = 0.0000133853271900 ASLP3 = 3.2462216641520829

BSLP4 = 0.0000033463317975 ASLP4 = -0.7584278523006615

DIGITAL SOFTWARE FOR SIMULATION - DIRECT FORM (SINUSOIDS AS INPUT)

71

C

A=12.52096/40.82834
 B=11.00999/45.28317
 D=1.04528317.57668
 E=1.04528317.57668
 F=1.04528317.57668
 A1=-2.+B*(1+.2)/2.
 B1=-2.+B*(1+.2)/2.
 C1=-2.+B*(1+.2)/2.
 D1=-2.+B*(1+.2)/2.
 E1=-2.+B*(1+.2)/2.
 F1=-2.+B*(1+.2)/2.
 G1=-2.+B*(1+.2)/2.
 H1=-2.+B*(1+.2)/2.
 I1=-2.+B*(1+.2)/2.

CODE IS "ASHP41" MEANS "A1 COEFFICIENT FOR THE SELECTABLE HIGH
 PASS FILTER WITH LOWER LIMIT 0.04 HZ"

ASHP41=-((G1*(A1*E1+B1*D1))+(H1*A1*D1))/(G1*A1*D1)
 ASHP42=-((G1*(A1*F1+B1*E1+C1*D1))+H1*(A1*E1+B1*D1))/(G1*A1*D1)
 ASHP43=-((G1*(B1*F1+C1*E1))+H1*(A1*F1+B1*E1+C1*D1))/(G1*A1*D1)
 ASHP44=-((G1*(C1*F1+H1*(B1*F1+C1*E1))+H1*(A1*F1+B1*E1+C1*D1))/(G1*A1*D1)
 ASHP45=-((H1*(C1*F1+H1*(B1*F1+C1*E1)))/(G1*A1*D1)
 ASHP46=-((H1*(C1*F1+H1*(B1*F1+C1*E1)))/(G1*A1*D1)
 BSHP41=-6./((G1*A1*D1)
 BSHP42=-15./((G1*A1*D1)
 BSHP43=-20./((G1*A1*D1)
 BSHP44=-15./((G1*A1*D1)
 BSHP45=-6./((G1*A1*D1)
 BSHP46=-1./((G1*A1*D1)

COEFFICIENTS FOR SELECTABLE LOW PASS FILTER WITH UPPER FREQ.
 OF 0.6 HZ

AA=1.033452
 BB=0.35804/C.03492
 CC=1.033452
 DD=1.033452
 EE=0.20696/0.02779
 FF=1.033452
 AA1=AA*1/4.
 BB1=BB*1/4.

CCCC

CCCC

APP00490
 APP00500
 APP00510
 APP00520
 APP00530
 APP00540
 APP00550
 APP00560
 APP00570
 APP00580
 APP00590
 APP00600
 APP00610
 APP00620
 APP00630
 APP00640
 APP00650
 APP00660
 APP00670
 APP00680
 APP00690
 APP00700
 APP00710
 APP00720
 APP00730
 APP00740
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 APP00760
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 APP00890
 APP00900
 APP00910
 APP00920
 APP00930
 APP00940
 APP00950
 APP00960


```

CC1=AA1 (T**2)/4.
DEE1=DD1
FF1=DD1 + BB*T/2. + CC*(T**2)/4.
GG1=(1.2. + CC*(T**2)/2. + CC*(T**2)/4.)
HH1=(1.2. - BB*T/2. + CC*(T**2)/4.)
II1=(1.2. + EE*T/2. + FF*(T**2)/4.)
JJ1=(1.2. + FF*(T**2)/2. + FF*(T**2)/4.)
KK1=(1.2. - EE*T/2. + FF*(T**2)/4.)
LL1=(1.2. - EE*T/2. + FF*(T**2)/4.)
ASLP61=-(GG1*KK1+HH1*JJ1)/(GG1*JJ1)
ASLP62=-(HH1*LL1+II1*KK1)/(GG1*JJ1)
ASLP63=-(II1*LL1)/(GG1*JJ1)
ASLP64=-(AA1*DD1+BB1*DEE1+CC1*FF1)/(GG1*JJ1)
BSLP60=(AA1*DEE1+BB1*DD1)/(GG1*JJ1)
BSLP61=(AA1*FF1+BB1*EE1+CC1*JJ1)/(GG1*JJ1)
BSLP62=(BB1*FF1+CC1*FF1)/(GG1*JJ1)
BSLP63=(CC1*FF1)/(GG1*JJ1)
BSLP64=(CC1*FF1)/(GG1*JJ1)

```

FINISHED COMPUTING COEFFICIENTS, INITIALIZE STORAGE REGISTERS

```

DO 200 J=1,3000
TRU(J)=0.
YD(J)=0.
YPO(J)=0.
ASQ(J)=0.
SIG(J)=0.
200 CONTINUE

```

STORAGE REGISTERS SET TO 0;
SET UP EQUATIONS FOR FILTER

```

DO 100 I=1,3000
I1=I-1
I2=I-2
I3=I-3
I4=I-4
I5=I-5
I6=I-6
IF(I1) I1=1
IF(I2) I2=1
IF(I3) I3=1
IF(I4) I4=1
IF(I5) I5=1
IF(I6) I6=1
AND I=GUBFS(DSEED)

```

APP00970
APP00980
APP00990
APP01000
APP01010
APP01020
APP01030
APP01040
APP01050
APP01060
APP01070
APP01080
APP01090
APP01100
APP01110
APP01120
APP01130
APP01140
APP01150
APP01160
APP01170
APP01180
APP01190
APP01200
APP01210
APP01220
APP01230
APP01240
APP01250
APP01260
APP01270
APP01280
APP01290
APP01300
APP01310
APP01320
APP01330
APP01340
APP01350
APP01360
APP01370
APP01380
APP01390
APP01400
APP01410
APP01420
APP01430
APP01440


```

APP01930
APP01940
APP01950
APP01960
APP01970
APP01980
APP01990
APP02000
APP02010
APP02020
APP02030
APP02040
APP02050

```

```

C      CALL DRAW(3000, TIME, ASQ, 0, 0, LABEL, TITLB, 0, 0, 0, 0, 0, 0, 5, 4, 1, LAST)
C      THIRD PLOT WILL BE A PLOT OF THE 'TRUE' SIGNAL VERSUS TIME
C      WITH SIGNAL ON THE X AXIS AND TIME ON THE Y AXIS
C      CALL DRAW(3000, TIME, YPO, 0, 0, LABEL, TITLC, 0, 0, 0, 0, 0, 5, 4, 1, LAST)
C      FINISHED PLOTTING
C      STOP
C      END
C      / *

```

APPENDIX F
DIGITAL SOFTWARE FOR SIMULATION - CASCADE FORM (SINUSOIDS AS INPUT)

```

//HUETE JOB (1457,1106), ' ', CLASS=B
//EXEC FRTXCLGP
//FORT.SYSIN DD *
CCCCCCCCCCCC

THIS PROGRAM IS DESIGNED TO TEST THE ACTION OF THE PRELIMINARY
DIGITAL FILTER PROGRAM FOR THE ASQ-81 BY INTRODUCING SIMULATED
MAGNETIC SIGNALS INTO THE SYSTEM THROUGH THE USE OF SINUSOIDS
OF VARYING FREQUENCY, BOTH WITHIN AND OUTSIDE THE FREQUENCY
RANGE OF THE FILTER, WITH RANDOM NOISE ADDED

SET UP ARRAYS. SIG() IS THE SIGNAL, ASQ() IS THE PROGRAM
OUTPUT, TRU() IS THE SIGNAL WITHIN THE FREQUENCY RANGE OF THE
PROGRAM

DIMENSION SIG(3000), ASQ(3000), TRU(3000), TIME(3000)
DIMENSION YQ(3000), YPO(3000)
DIMENSION XI(3000), XII(3000), XIII(3000), XIV(3000), XV(3000)
REAL*8 DSEEC
REAL*8 T, AFHP1, AFHP2, BFHP0, BFHP1, BFHP2, A, B, C, D, E, F
REAL*8 A1, B1, C1, D1, E1, F1, G1, H1, I1, J1, K1, L1
REAL*8 AA, BB, CC, DD, EE, FF, AA1, BB1, CC1, DD1, EE1, FF1, GG1, HH1, I11
REAL*8 JJ1, KK1, LL1
REAL*8 ASHP41, ASHP42, ASHP43, ASHP44, ASHP45, ASHP46, ASHP47
REAL*8 ASLP61, ASLP62, ASLP63, ASLP64
REAL*8 BSLP60, BSLP61, BSLP62, BSLP63, BSLP64
REAL*8 TITL A(12), HUETE
$8*
REAL*8 TITL B(12), HUETE
$8*
REAL*8 TITL C(12), HUETE
$8*
REAL*8 TITL D(12), HUETE
$8*
REAL*8 TITL E(12), HUETE
$8*
REAL LABEL, ' '
DATA PI/3.141592954/
DOUBLE PRECISION DSEED

DEFINE AND COMPUTE ALL COEFFICIENTS
TEN SAMPLES PER SECOND

T=1./10.

COEFFICIENTS FOR FIXED HIGH PASS FILTER

AFHP1=-((T**2/160.-2.)/(1.+T/8.+T**2/320.))
AFHP2=-((1.-T/8.+T**2/320.)/(1.+T/8.+T**2/320.))

```

APP02560
 APP02570
 APP02580
 APP02590
 APP02600
 APP02610
 APP02620
 APP02630
 APP02640
 APP02650
 APP02660
 APP02670
 APP02680
 APP02690
 APP02700
 APP02710
 APP02720
 APP02730
 APP02740
 APP02750
 APP02760
 APP02770
 APP02780
 APP02790
 APP02800
 APP02810
 APP02820
 APP02830
 APP02840
 APP02850
 APP02860
 APP02870
 APP02880
 APP02890
 APP02900
 APP02910
 APP02920
 APP02930
 APP02940
 APP02950
 APP02960
 APP02970
 APP02980
 APP02990
 APP03000
 APP03010
 APP03020
 APP03030

BFHP0=(1./1.+T/8.+T**2/320.))
 BFHP1=-2./1.+T/8.+T**2/320.))
 BFHP2=(1./1.+T/8.+T**2/320.))
 COEFFICIENTS FOR SELECTABLE HIGH PASS FILTER
 IN THIS CASE, F(LOWER)=0.04 HZ

A=12.52096/40.82834
 B=1./40.82834
 C=11.00999/45.28317
 D=1./45.28317
 E=7.41498/57.57668
 F=1./57.57668
 A1=1.+A*T/2.+B*(T**2)/4.
 B1=-2.+B*T/2.+B*(T**2)/4.
 C1=1.-A*T/2.+B*(T**2)/4.
 D1=1.+C*T/2.+D*(T**2)/4.
 E1=-2.+D*T/2.+D*(T**2)/4.
 F1=1.-C*T/2.+D*(T**2)/4.
 G1=1.+E*T/2.+F*(T**2)/4.
 H1=-2.+F*(T**2)/4.
 I1=1.-E*T/2.+F*(T**2)/4.

CODE IS "ASHP41" MEANS "A1 COEFFICIENT FOR THE SELECTABLE HIGH
 PASS FILTER WITH LOWER LIMIT 0.04 HZ"

ASHP41=1./1.(A1/D1*G1)
 ASHP42=-1.(C1/A1)
 ASHP43=-1.(B1/A1)
 ASHP44=-1.(E1/D1)
 ASHP45=-1.(F1/D1)
 ASHP46=-1.(H1/G1)
 ASHP47=-1.(I1/G1)

COEFFICIENTS FOR SELECTABLE LOW PASS FILTER WITH UPPER FREQ.
 OF 0.6 HZ

AA=1./0.03492
 BB=0.35804/C.03492
 CC=1./0.03492
 DD=1./0.02779
 EE=0.20696/0.02779
 FF=1./0.02779
 AA1=AA*(T**2)/4.
 BB1=2.*AA1
 CC1=AA1
 DD1=DD*(T**2)/4.
 EE1=2.*DD1

```

APP03040
APP03050
APP03060
APP03070
APP03080
APP03090
APP03100
APP03110
APP03120
APP03130
APP03140
APP03150
APP03160
APP03170
APP03180
APP03190
APP03200
APP03210
APP03220
APP03230
APP03240
APP03250
APP03260
APP03270
APP03280
APP03290
APP03300
APP03310
APP03320
APP03330
APP03340
APP03350
APP03360
APP03370
APP03380
APP03390
APP03400
APP03410
APP03420
APP03430
APP03440
APP03450
APP03460
APP03470
APP03480
APP03490
APP03500
APP03510

FF1=DD1+BB*T/2.+CC*(T**2)/4.)
GG1=((1.-2.+CC*(T**2)/2.)**2)/4.)
HH1=((1.-BB*T/2.+CC*(T**2)/4.)**2)/4.)
II1=((1.-EE*T/2.+FF*(T**2)/2.)**2)/4.)
JJ1=((1.-EE*T/2.+FF*(T**2)/2.)**2)/4.)
KK1=((1.-EE*T/2.+FF*(T**2)/2.)**2)/4.)
LL1=((1.-EE*T/2.+FF*(T**2)/2.)**2)/4.)
ASLP61=((GGI*KK1+HHI*KK1)/(GGI*JJ1))
ASLP62=((GGI*LL1+HHI*KK1)/(GGI*JJ1))
ASLP63=((HHI*LL1+II*JJ1)/(GGI*JJ1))
ASLP64=((II*LL1)/(GGI*JJ1))
BSLP60=((AAI*DEI+BBI*DEI)/(GGI*JJ1))
BSLP61=((AAI*EEI+BBI*EEI)/(GGI*JJ1))
BSLP62=((AAI*FFI+BBI*FFI)/(GGI*JJ1))
BSLP63=((BBI*FFI+CCI*FFI)/(GGI*JJ1))
BSLP64=((CCI*FFI)/(GGI*JJ1))

FINISHED COMPUTING COEFFICIENTS, INITIALIZE STORAGE REGISTERS

DO 200 J=1,3000
TRU(J)=0.
YD(J)=0.
YPQ(J)=0.
ASQ(J)=0.
SIG(J)=0.
CONTINUE

STORAGE REGISTERS SET TO 0, EQUATIONS FOR SIMULATED SIGNAL

DSSEED = 1456.
PHI1=GGUBFS(DSEED)*2.*PI
PHI2=GGUBFS(DSEED)*2.*PI
DO 100 I=1,3000
I1=1-1
I2=1-2
I3=1-3
I4=1-4
I5=1-5
I6=1-6
IF(I1) I1=1
IF(I2) I2=1
IF(I3) I3=1
IF(I4) I4=1
IF(I5) I5=1
IF(I6) I6=1
TRU(I)=SIN(0.02*PI*FLOAT(I)+PHI1)
ANOI=GGUBFS(DSEED)

```


APPENDIX G

DIGITAL SOFTWARE FOR COMPUTATION OF SYSTEM AMPLITUDE VERSUS FREQUENCY

APP04100
APP04110
APP04120
APP04130
APP04140
APP04150
APP04160
APP04170
APP04180
APP04190
APP04200
APP04210
APP04220
APP04230
APP04240
APP04250
APP04260
APP04270
APP04280
APP04290
APP04300
APP04310
APP04320
APP04330
APP04340
APP04350
APP04360
APP04370
APP04380
APP04390
APP04400
APP04410
APP04420
APP04430
APP04440
APP04450
APP04460
APP04470
APP04480
APP04490
APP04500
APP04510
APP04520
APP04530
APP04540
APP04550
APP04560
APP04570

```
//HUETE JOB (1457,1106), ' ', CLASS=B
// EXEC FRTXCLGP
// FORT.SYSIN DD *
CCCCCCCCCCCCC
      MGN4 FORTRAN
      THIS PROGRAM IS DESIGNED TO INPUT VARIOUS FREQUENCIES INTO THE
      DIGITAL FILTER PROGRAM FOR THE ASQ-81 AND OBTAIN THE DB LOSS
      CHARACTERISTIC FOR COMPARISON WITH MEASURED DB LOSSES FOR THE
      ASQ 81 MAGNETOMETER. A SINGLE FREQUENCY SIGNAL WILL BE INPUTTED
      AND THE RMS OUTPUT DIVIDED BY THE RMS INPUT TO DETERMINE
      ATTENUATION
      SET UP ARRAYS. SIG() IS THE SIGNAL, ASQ() IS THE PROGRAM
      OUTPUT, TRU() IS THE SIGNAL WITHIN THE FREQUENCY RANGE OF THE
      PROGRAM
      DIMENSION SIG(3000), ASQ(3000), TRU(3000), TIME(3000)
      DIMENSION YG(3000), YPO(3000), FREQ(20)
      DIMENSION XI(3000), XII(3000), XIII(3000), XIV(3000), XV(3000)
      REAL*8 DSEED
      REAL*8 T, AFHP1, AFHP2, BFHP0, BFHP1, BFHP2, A, B, C, D, E, F
      REAL*8 AI, BI, CI, DI, EI, FI, GI, HI, II, JI, KI, LI
      REAL*8 AA, BB, CC, DD, EE, FF, AA1, BB1, CC1, DD1, EE1, FF1, GG1, HH1, II1
      REAL*8 JJ1, KK1, LLL1
      REAL*8 ASHP41, ASHP42, ASHP43, ASHP44, ASHP45, ASHP46, ASHP47
      REAL*8 ASLP61, ASLP62, ASLP63, ASLP64
      REAL*8 BSLP60, BSLP61, BSLP62, BSLP63, BSLP64
      DATA PI/3.141592954/
      DOUBLE PRECISION DSEED, SUMSQ, SMSQT, RATIO
      DEFINE AND COMPUTE ALL COEFFICIENTS
      TEN SAMPLES PER SECOND
      T=1./10.
      COEFFICIENTS FOR FIXED HIGH PASS FILTER
      AFHP1=-((T**2/160.-2.)/(1.+T/8.+T**2/320.))
      AFHP2=-((1.-T/8.+T**2/320.)/(1.+T/8.+T**2/320.))
      BFHP0=(1.)/(1.+T/8.+T**2/320.))
      BFHP1=-((2.)/(1.+T/8.+T**2/320.))
      BFHP2=(1.)/(1.+T/8.+T**2/320.))
      COEFFICIENTS FOR SELECTABLE HIGH PASS FILTER
      IN THIS CASE, F(LOWER)=0.04 HZ
      A=12.52096/40.82834
      B=1./40.82834
      C=11.00999/45.28317
      D=1./45.28317
CCCCCCCCCCCCC
```

APP04580
 APP04590
 APP04600
 APP04610
 APP04620
 APP04630
 APP04640
 APP04650
 APP04660
 APP04670
 APP04680
 APP04690
 APP04700
 APP04710
 APP04720
 APP04730
 APP04740
 APP04750
 APP04760
 APP04770
 APP04780
 APP04790
 APP04800
 APP04810
 APP04820
 APP04830
 APP04840
 APP04850
 APP04860
 APP04870
 APP04880
 APP04890
 APP04900
 APP04910
 APP04920
 APP04930
 APP04940
 APP04950
 APP04960
 APP04970
 APP04980
 APP04990
 APP05000
 APP05010
 APP05020
 APP05030
 APP05040
 APP05050

E=7.41458/57.5766E
 F=1./57.57668
 A1=1.+A*(T**2/2.+B*(T**2)/4.
 B1=1.-A*(T**2/2.+B*(T**2)/4.
 C1=1.-A*(T**2/2.+D*(T**2)/4.
 D1=1.-C*(T**2/2.+D*(T**2)/4.
 E1=1.-C*(T**2/2.+F*(T**2)/4.
 G1=1.-E*(T**2/2.+F*(T**2)/4.
 H1=1.-E*(T**2/2.+F*(T**2)/4.
 I1=1.-E*(T**2/2.+F*(T**2)/4.

 CODE IS "ASHP41" MEANS "A1 COEFFICIENT FOR THE SELECTABLE HIGH
 PASS FILTER WITH LOWER LIMIT 0.04 HZ"

 ASHP41=1./((A1*D1*G1)
 ASHP42=-((C1/A1)
 ASHP43=-((B1/A1)
 ASHP44=-((E1/D1)
 ASHP45=-((F1/D1)
 ASHP46=-((H1/G1)
 ASHP47=-((I1/G1)

 COEFFICIENTS FOR SELECTABLE LOW PASS FILTER WITH UPPER FREQ.
 OF 0.6 HZ

 AA=1./0.03492
 BB=0.35804/C.03492
 CC=1./0.03492
 DD=1./0.02779
 EE=0.20696/0.02779
 FF=1./0.02779
 AA1=AA*(T**2)/4.
 BB1=2.*AA1
 CC1=AA1
 DD1=DD*(T**2)/4.
 EE1=2.*DD1
 FF1=DD1
 GG1=(1.-BB*(T**2/2.+CC*(T**2)/4.)
 HH1=(1.-CC*(T**2/2.+DD*(T**2)/4.)
 II1=(1.-BB*(T**2/2.+CC*(T**2)/4.)
 JJ1=(1.-EE*(T**2/2.+FF*(T**2)/4.)
 KK1=(1.-EE*(T**2/2.+FF*(T**2)/4.)
 LL1=(1.-EE*(T**2/2.+FF*(T**2)/4.)
 ASLP61=-((GG1*KK1+HH1*JJ1)/(GG1*JJ1)
 ASLP62=-((GG1*LL1+HH1*KK1)/(GG1*JJ1)
 ASLP63=-((HH1*LL1+II1*KK1)/(GG1*JJ1)
 ASLP64=-((II1*LL1)/(GG1*JJ1)

CCCC

CCCC

```

APP05060
APP05070
APP05080
APP05090
APP05100
APP05110
APP05120
APP05130
APP05140
APP05150
APP05160
APP05170
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APP05190
APP05200
APP05210
APP05220
APP05230
APP05240
APP05250
APP05260
APP05270
APP05280
APP05290
APP05300
APP05310
APP05320
APP05330
APP05340
APP05350
APP05360
APP05370
APP05380
APP05390
APP05400
APP05410
APP05420
APP05430
APP05440
APP05450
APP05460
APP05470
APP05480
APP05490
APP05500
APP05510
APP05520
APP05530

```

```

BSLP60=(AA1*DD1)/(GG1*JJ1)
BSLP61=(AA1*EE1+BB1*DD1)/(GG1*JJ1)
BSLP62=(AA1*FF1+BB1*EE1+CC1*DD1)/(GG1*JJ1)
BSLP63=(BB1*FF1+CC1*EE1)/(GG1*JJ1)
BSLP64=(CC1*FF1)/(GG1*JJ1)

```

FINISHED COMPUTING COEFFICIENTS, INITIALIZE STORAGE REGISTERS

```

DO 200 J=1,2000
  TRU(J)=0.
  YD(J)=0.
  YPO(J)=0.
  ASQ(J)=0.
  SIG(J)=0.
  CONTINUE

```

200

STORAGE REGISTERS SET TO 0, EQUATIONS FOR SIMULATED SIGNAL

```

DSEED = 1456.
PHI1=GGURFS(DSEED)*2.*PI
PHI2=GGURFS(DSEED)*2.*PI
FREQ(1)=0.01
FREQ(2)=0.02
FREQ(3)=0.03
FREQ(4)=0.04
FREQ(5)=0.05
FREQ(6)=0.06
FREQ(7)=0.07
FREQ(8)=0.08
FREQ(9)=0.09
FREQ(10)=0.10
FREQ(11)=0.20
FREQ(12)=0.30
FREQ(13)=0.40
FREQ(14)=0.50
FREQ(15)=0.60
FREQ(16)=0.70
FREQ(17)=0.80
FREQ(18)=0.90
FREQ(19)=1.0
FREQ(20)=1.15
DO 300 I=1,20
  DO 100 I=1,3000
    I1=I-1
    I2=I-2
    I3=I-3
    I4=I-4
    I5=I-5

```

CC

CC

```

APP05540
APP05550
APP05560
APP05570
APP05580
APP05590
APP05600
APP05610
APP05620
APP05630
APP05640
APP05650
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APP05670
APP05680
APP05690
APP05700
APP05710
APP05720
APP05730
APP05740
APP05750
APP05760
APP05770
APP05780
APP05790
APP05800
APP05810
APP05820
APP05830
APP05840
APP05850
APP05860
APP05870
APP05880
APP05890
APP05900
APP05910
APP05920
APP05930
APP05940
APP05950
APP05960
APP05970
APP05980
APP05990
APP06000
APP06010

```

```

16=1-6
IF(I1.LT.1)I1=1
IF(I2.LT.1)I2=1
IF(I3.LT.1)I3=1
IF(I4.LT.1)I4=1
IF(I5.LT.1)I5=1
IF(I6.LT.1)I6=1
TRIG(I1)=TRIG(I)
TIME(I)=FLOAT(I)/600.

THE FIRST STAGE OF THE FILTER PROGRAM IS COMMENTED OUT BECAUSE IN
THIS VERSION OF THE PROGRAM THE FIXED HIGH PASS FILTER IS NOT
INCLUDED SO AS TO ENABLE COMPARISON WITH DATA FURNISHED BY
TEXAS INSTRUMENTS, INC. BY REMOVING THE COMMENT CHARACTERS, AND
COMMENTING OUT THE STEP FOLLOWING THEM ( YO(I)=SIG(I), THE
PROGRAM CAN BE MADE TO INCLUDE THE FIXED HIGH PASS FILTER

YO(I)=BFHPO*SIG(I)+BFHP1*SIG(I1)+BFHP2*SIG(I2)+AFHP1*YO(I1)
$+AFHP2*YO(I2)
YO(I1)=SIG(I)
XI(I1)=ASHP41*YO(I1)+ASHP42*XI(I2)+ASHP43*XI(I1)
XI(I2)=-2.*XI(I1)
XI(I1)=XI(I1)+ASHP44*XI(I1)+ASHP45*XI(I2)
XI(I2)=-2.*XI(I1)+XI(I2)
XV(I1)=XIV(I1)+ASHP46*XV(I1)+ASHP47*XV(I2)
XV(I2)=-2.*XV(I1)
YPO(I1)=XV(I1)+XV(I2)
GP1=ASLP61*ASQ(I1)+ASLP62*ASQ(I2)+ASLP63*ASQ(I3)+ASLP64*ASQ(I4)
GP2=BSLP60*YPO(I1)+BSLP61*YPO(I1)+BSLP62*YPO(I2)
$+BSLP63*YPO(I3)+BSLP64*YPO(I4)
ASQ(I)=GP1+GP2

100 CONTINUE

THE FOLLOWING SECTION COMPUTES THE AVERAGE VALUES OF THE OUTPUT
AND CONVERTS TO DB ATTENUATION

SUMSQ=0.0
SMSQT=0.0
DO 301 JJ=2000,3000
SUMSQ=SUMSQ+{ASQ(JJ)**2}
SMSQT=SMSQT+{TRU(JJ)**2}
CONTINUE
RATIO=SUMSQ/SMSQT
DBLOSS=10.*DLOG10(RATIO)
WRITE(6,401)FREQ(I),DBLOSS
FORMAT(IX, FREQNCY = ,F10.2, DB LOSS = , F10.5)

```

APP06020
APP06030
APP06040
APP06050
APP06060
APP06070
APP06080

CC FINISHED PLCTING
CC 300 CONTINUE
/* STOP
END


```

CCC
BFH92=(1./(1.+T/8.+T**2/32G.))
COEFFICIENTS FOR SELECTABLE HIGH PASS FILTER
IN THIS CASE, F(LOWER)=0.04 HZ
A=12.52096/40.82834
B=1./40.82834
C=11.00999/45.28517
D=1./45.28317
E=7.41459/57.57663
F=1./57.27663
A1=1.+A*T/2.+B*(T**2)/4.
B1=-2.+B*(T**2)/2.
C1=1.-A*T/2.+B*(T**2)/4.
D1=1.-C*T/2.+D*(T**2)/4.
E1=-2.+D*(T**2)/2.
F1=1.-E*T/2.+F*(T**2)/4.
G1=1.-F*(T**2)/2.
H1=-2.+F*(T**2)/2.
I1=1.-E*T/2.+F*(T**2)/4.
CODE IS "ASHP41" MEANS "A1 COEFFICIENT FOR THE SELECTABLE HIGH
PASS FILTER WITH LOWER LIMIT 0.04 HZ"
ASHP41=1./((A1/D1*G1))
ASHP42=-((C1/A1))
ASHP43=-((B1/A1))
ASHP44=-((E1/D1))
ASHP45=-((F1/D1))
ASHP46=-((H1/G1))
ASHP47=-((I1/G1))
COEFFICIENTS FOR SELECTABLE LOW PASS FILTER WITH UPPER FREQ.
OF 0.6 HZ
AA=1./0.03492
BB=0.35804/C.03492
CC=1./0.03492
DD=1./0.02779
EE=0.20696/C.02779
FF=1./0.02779
AA1=A*(T**2)/4.
BB1=2.*AA1
CC1=AA1
DD1=DD*(T**2)/4.
EE1=2.*DD1
FF1=DD1
GG1=(1.+BB*T/2.+CC*(T**2)/4.)
APP06590
APP06600
APP06610
APP06620
APP06630
APP06640
APP06650
APP06660
APP06670
APP06680
APP06690
APP06700
APP06710
APP06720
APP06730
APP06740
APP06750
APP06760
APP06770
APP06780
APP06790
APP06800
APP06810
APP06820
APP06830
APP06840
APP06850
APP06860
APP06870
APP06880
APP06890
APP06900
APP06910
APP06920
APP06930
APP06940
APP06950
APP06960
APP06970
APP06980
APP06990
APP07000
APP07010
APP07020
APP07030
APP07040
APP07050
APP07060

```

APP07070
APP07080
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APP07110
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APP07390
APP07400
APP07410
APP07420
APP07430
APP07440
APP07450
APP07460
APP07470
APP07480
APP07490
APP07500
APP07510
APP07520
APP07530
APP07540

```

HH1=(-2.+CC*(T**2)/2.+CC*(T**2)/4.)
II1=(1.-BB*T/2.+CC*(T**2)/4.)
JJ1=(1.+EE*T/2.+FF*(T**2)/4.)
KK1=(-2.+FF*(T**2)/2.+FF*(T**2)/4.)
LL1=(1.-EE*T/2.+FF*(T**2)/4.)
ASLP61=-((GG1*KK1+HH1*JJ1)/(GG1*JJ1))
ASLP62=-((GG1*LL1+HH1*KK1+II1*JJ1)/(GG1*JJ1))
ASLP63=-((HH1*LL1+II1*KK1)/(GG1*JJ1))
ASLP64=-((II1*LL1)/(GG1*JJ1))
BSLP60=(AA1*DD1)/(GG1*JJ1)
BSLP61=(AA1*EE1+BB1*DD1)/(GG1*JJ1)
BSLP62=(AA1*FF1+BB1*EE1+CC1*DD1)/(GG1*JJ1)
BSLP63=(BB1*FF1+CC1*EE1)/(GG1*JJ1)
BSLP64=(CC1*FF1)/(GG1*JJ1)

```

FINISHED COMPUTING COEFFICIENTS, INITIALIZE STORAGE REGISTERS

```

DO 200 J=1,3000
  TRU(J)=0.
  YPO(J)=0.
  YPO(J)=0.
  ASQ(J)=0.
  SIG(J)=0.
  200 CONTINUE

```

STORAGE REGISTERS SET TO 0, EQUATIONS FOR SIMULATED SIGNAL

```

DO 100 I=1,2400
  I1=I-1
  I2=I-2
  I3=I-3
  I4=I-4
  I5=I-5
  I6=I-6
  IF(I1.LT.1)I1=1
  IF(I2.LT.1)I2=1
  IF(I3.LT.1)I3=1
  IF(I4.LT.1)I4=1
  IF(I5.LT.1)I5=1
  IF(I6.LT.1)I6=1

```

THIS SIGNAL STATEMENT INPUTS A 180 KNOTS AIRCRAFT AT A CPA RANGE OF 400 FEET: THIS IS TO TEST THE OPERATION OF THE SELCE TABLE LOW PASS FILTER SECOND ANDERSON FUNCTION 8 HZ FILTER

```

TIME(I)=FLOAT(I)/480.
BETA=18000.*(TIME(I)-2.5)/400.

```



```
CALL DRAW(2400,TIME,ASQ,0,0,LABEL,TITLE,0,0,0,0,0,0,10,4,1,LAST)
THIRD PLOT WILL BE A PLOT OF THE TRUE SIGNAL VERSUS TIME
WITH SIGNAL ON THE X AXIS AND TIME ON THE Y AXIS
CALL DRAW(2400,TIME,YPO,0,0,LABEL,TITLE,0,0,0,0,0,0,10,4,1,LAST)
CALL DRAW(2400,TIME,SIG,0,0,LABEL,TITLE,0,0,0,0,0,0,10,4,1,LAST)
FINISHED PLOTTING
STOP
END
```

UUUU UU /

APPENDIX I DIGITAL FILTERING SOFTWARE

```

//HUETE JOB (1457,0165), 'HUETE      SMC 2740', CLASS=G
//*MAIN LINES=(65)
//EXEC FRTXCLGP; PARM=LKED='LIST,MAP,XREF',REGION.GO=2048K
//FORT. SYSIN DD
INTEGER*2 IN(16)
C      ARRAY 'IN' IS USED IN READING DATA FROM TAPE
C      COMPLEX*8 XX(8192)
C      REAL*4 ZZ(8192),YY(8192),XXP(8192)
C      THE ABOVE COMPLEX*8 ARRAYS ARE USED TO ORDER INPUT DATA AND
C      INITIALLY REPRESENT VOLTAGE - TIME SERIES INFORMATION.
C
C      THE NEXT THREE LINES ARE ARRAYS NEEDED FOR DATA TAPE READING AND
C      CONVERSION TO TOTAL FIELD FLUCTUATION TIME SERIES
C      DIMENSION TIME(8192),FREQ(8192),WORK(24576),FRQ2(8192)
C      DIMENSION ZX1(8192),ZY1(8192)
C      DIMENSION ZZX1(24576),ZZY1(24576),ZZV1(24576)
C
C      THE FOLLOWING LINES CONTAIN ARRAYS NEEDED FOR SIGNAL INPUT TO THE
C      FILTER; SIGNAL PROCESSING WITHIN THE FILTER, AND COEFFICIENTS
C      USED BY THE FILTER PROGRAM
C      DIMENSION TIME2(24576),OUTFLD(24576),CLFLD(24576)
C      REAL*8 AH(4),BH(4),CH(4),DH(4),EH(4),FH(4),FRQH(4),FRQL(3)
C      REAL*8 AL(3),BL(3),CL(3),DL(3),EL(3),FL(3),FL(3),FRQL(3)
C      REAL*8 T1,AFHPI1,BFHP2,BFHP3,BFHP4,BFHP5,ASHP6,ASHP7
C      REAL*8 I1,J1,K1,L1,ASHP1,ASHP2,ASHP3,ASHP4,ASHP5,ASHP6,ASHP7
C      REAL*8 ASLP1,ASLP2,ASLP3,ASLP4,ASLP5,ASLP6,ASLP7,BSLP1,BSLP2,BSLP3,BSLP4
C      REAL*8 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APP08660
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APP09110
APP09120
APP09130

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SET VARIABLES EQUAL TO ZERO

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DATA XX/8192*0.0.0.//
DATA ZZ/VV/16384*0.//
DATA 7X1/8192*0.//
DATA TIME,FREQ/16384*0.//
K=0
I4=1
I5=1
CONSTX=0.0
SUMX=0.0
SUMY=0.0
SUMZ=0.0
AVEI=0.0
XORIGP=0.0
XMAXP=0.0

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SET STORAGE REGISTERS TO ZERO. STORAGE REGISTERS ARE USED VICE
INTERMEDIATE OUTPUT ARRAYS IN ORDER TO CUT DOWN THE AMOUNT OF
ARRAY STORAGE REQUIRED BY THE PROGRAM AND TO RETAIN "MEMORY"
OF PREVIOUS VALUES FOR COMPUTATIONAL USE IN ORDER TO ELIMINATE
THE "START UP" LAG OF THE OUTPUT VALUES

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SIG2=0.0
SIG1=0.0
Y02=0.0
Y01=0.0
X12=0.0
X11=0.0
X111=0.0
XV2=0.0
XV1=0.0
YPO4=0.0
YPO3=0.0
YPO2=0.0
YPO1=0.0
OUTFD4=0.0
OUTFD3=0.0
OUTFD2=0.0
OUTFD1=0.0

```

THE FOLLOWING SEVERAL STEPS WOULD BE USED IF THE INPUT TO THE
FILTER PROGRAM WERE THREE MUTUALLY PERPENDICULAR COIL SENSORS.
SINCE THE INPUT IS A SINGLE COIL SENSOR ORIENTED ALONG THE
EARTH'S FIELD, THESE STEPS ARE NOT NECESSARY, BUT ARE RETAINED
AS REFERENCE

CC

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APP09140
 APP09150
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 APP09580
 APP09590
 APP09600
 APP09610

```

      TWOPI=6.2831853
      COS60=COS(TWOPI/6.)
      COS30=COS(TWOPI/12.)
      D=16.75*TWOPI/360.
      COSD=COS(D)
      COSDI=COS(D)
      COSDI=COS(D)
      D IS THE DECLINATION OR MAGNETIC VARIATION AT THE MAGNETOMETER
      SITE.

      SET ARRAYS TO ZERO
      DO 31 IN1=1,24576
      ZZ XI(IN1)=0.0
      ZZ YI(IN1)=0.0
      ZZ VI(IN1)=0.0
      TIME2(IN1)=0.0
      CONTINUE
31  THE NEXT FIVE LINES SERVE AS A TIME DELAY IN STARTING THE
      DATA ANALYSIS
      ISEC=10
      IFL=1
      JJ=1, IFL
      CALL RD(20, IN, 200, IREC, IRR)
55  CONTINUE=8192
      NR=1
      FNR=FLOAT(NR)
      DO 200 IM=1, NR
      XORIGP=XMAXP
      DO 70 IL=1, 3
      THE DO LOOP ENDING WITH STATEMENT 70 ENABLES THE PROGRAM TO
      PROCESS A LARGE AMOUNT OF DATA BY REPEATING THE PROCESS IN
      BLOCKS. THE DATA POINTS FROM EACH RUN THROUGH THE DO LOOP ARE
      ADDED TOGETHER AND EVENTUALLY AVERAGED BY THE NUMBER OF RUNS
      THROUGH THE DO LOOP.
      NR REPRESENTS THE NUMBER OF DATA SEQUENCES TO BE AVERAGED.
      1 SEQUENCE CURRENTLY EQUALS 24576 DATA POINTS OR THREE SETS
      OF 128 SECONDS OF DATA.

      THE DO LOOP ENDING WITH 60 READS THE DATA FROM THE PCM FRAME
      STRIPS OUT THE SYNC CODE, AND SORTS OUT THE DATA BY COIL
      CHANNEL
      DO 60 JJ=1, IFRAME
      CALL RD(20, IN, 1000, IREC, IRR)
      XX(JJ)=IN(2)
      YY(JJ)=IN(3)
      ZZ(JJ)=IN(4)
      CONTINUE
60
  
```

CCCCC

CC

CCCCCCCCCCCCC

```

CCCCCCCC
200 WRITE(6,200)IRR,IREC
    FORMAT(10X,'IRR=',I6,5X,'IREC=',I6,/)
    THE FOLLOWING SECTION GENERATES THE TIME AND FREQUENCY
    ARRAYS AND NORMALIZES THE INPUT PCM DATA TO VOLTAGE FORM
    IN PREPARATION FOR FAST FOURIER TRANSFORM TO THE FREQUENCY
    DOMAIN.
    N=8192
    FN=FLOAT(N)
    DELTAT=1./64.
    DELTAF=1./((FN*DELTAT)
    DO 20 J=1,N
        TIME(J)=DELTAT*FLOAT(J)
        FREQ(J)=DELTAF*FLOAT(J)
        XX(J)=(XX(J)-2048.)*5./2048.
        XX(J)=REAL(XX(J))
        XXP(J)=XX(J)
        YY(J)=(YY(J)-2048.)*5./2048.
        ZZ(J)=(ZZ(J)-2048.)*5./2048.
    IN THIS USE OF THE PROGRAM, DATA 'YY' IS THE ASQ-81 DATA
    'XX' IS THE COIL ANTENNA COIL DATA, AND 'IF' IS THE
    'ZZ' IS THE SCHEDULED FIELD VECTOR.
    TOTAL GEOMETRICALLY PERPENDICULAR COIL SENSORS ARE USED, THIS
    IF THREE MUTUALLY PERPENDICULAR COIL SENSORS ARE USED, THIS
    WILL NOT BE TRUE. SEE REFERENCE 9 FOR HOW TO HANDLE THIS
CCCCCCCC
20 CONTINUE
DO 21 J=1,N
    FREQ(J)=ALOG10(FREQ(J))
21 CONTINUE
    THE NEXT FOUR STATEMENTS PERFORM AN FFT ON THE INPUT
    TIME SERIES DATA. SEE THE WRITEUP ON 'FOUR' FOR
    FURTHER INFORMATION.
    CALL FOURT(XX,N,1,0,WORK)
    THE NEXT BLOCK OF STATEMENTS APPLY THE SYSTEM (VOLTAGE TO
    B-FIELD) TRANSFER FUNCTION TO THE TRANSFORMED FREQUENCY
    DOMAIN DATA. THIS BLOCK ENDS AT STATEMENT 9.
    THE TRANSFER FUNCTION CONVERTS VOLTS TO NANOTESLAS (GAMMAS).
    ***WARNING*** THIS TRANSFER FUNCTION YIELDS AN INACCURATE
    PHASE. USE A DIFFERENT TRANSFER FUNCTION IF PHASE INFORMATION
    IS NEEDED.
    DO 9 L=1,N
        FREQ=L*DELTAF
        IF (FREQ.LE.2.5) GO TO 1
        XX(L)=XX(L)/28.
        GO TO 8
    1 IF (FREQ.LE.15) GO TO 2
      IF XX(L)=XX(L)/(105.5-3.14*FREQ)

```

```

APP09620
APP09630
APP09640
APP09650
APP09660
APP09670
APP09680
APP09690
APP09700
APP09710
APP09720
APP09730
APP09740
APP09750
APP09760
APP09770
APP09780
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APP09800
APP09810
APP09820
APP09830
APP09840
APP09850
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APP09880
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APP09930
APP09940
APP09950
APP09960
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APP09980
APP09990
APP10000
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APP10040
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APP10060
APP10070
APP10080
APP10090

```

APP1 0100
 APP1 0110
 APP1 0120
 APP1 0130
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 APP1 0170
 APP1 0180
 APP1 0190
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 APP1 0210
 APP1 0220
 APP1 0230
 APP1 0240
 APP1 0250
 APP1 0260
 APP1 0270
 APP1 0280
 APP1 0290
 APP1 0300
 APP1 0310
 APP1 0320
 APP1 0330
 APP1 0340
 APP1 0350
 APP1 0360
 APP1 0370
 APP1 0380
 APP1 0390
 APP1 0400
 APP1 0410
 APP1 0420
 APP1 0430
 APP1 0440
 APP1 0450
 APP1 0460
 APP1 0470
 APP1 0480
 APP1 0490
 APP1 0500
 APP1 0510
 APP1 0520
 APP1 0530
 APP1 0540
 APP1 0550
 APP1 0560
 APP1 0570

```

      GO TO 8
2  IF (FRQ.LE.10.)GO TO 3
   XX(L)=XX(L)/(5.958*FRQ-30.97)
   GO TO 8
3  IF (FRQ.LE.7.5)GO TO 4
   XX(L)=XX(L)/(3.492*FRQ-6.31)
   GO TO 8
4  IF (FRQ.LE.5.)GO TO 5
   XX(L)=XX(L)/(2.6311*FRQ+0.14667)
   GO TO 8
5  IF (FRQ.LE.3.)GO TO 6
   XX(L)=XX(L)/(2.6311*FRQ+0.14667)
   GO TO 8
6  XX(L)=XX(L)/(2.72*FRQ)
   GO TO 8
8  CONTINUE
9  CALL FOURT(XX,N,1,1,1,WORK)
   DO 57 J=1,N
   XX(J)=XX(J)/FN
57  CONTINUE
   WRITE(6,600)(XX(I),I=1,100)
   FORMAT(1X,F20.4,4X,F20.4)
   C THE FOLLOWING BLOCK TAKES THE MAGNITUDE OF THE COMPLEX VALUES
   C 600
   DO 56 I=1,N
   ZX(I)=CABS(XX(I))
   CONTINUE
56  IF (K.NE.0) GO TO 36
   SUMX=ZX(I)+SUMX
   CONTINUE
66  CONSTX=SUMX/144.
   DO 67 IS=1,8192
   ZX(I+1)=ZX(I)
   I=I+1
   CONTINUE
67  GO TO 37
36  CONTINUE
   SUMX=0.
   DO 68 IS=1,144
   SUMX=ZX(I)+SUMX
   CONTINUE
68  AVE!=SUMX/144.
   DO 69 IS=1,8192
   ZX(I+1)=ZX(I)+(CONSTX-AVE)
   I=I+1
   CONTINUE
69  CONTINUE
  
```



```

CCCCCCCCCCCC CCCC
REAL*8 AH(4),BH(4),CH(4),DH(4),EH(4),FH(4)
REAL*8 AL(3),BL(3),CL(3),DL(3),EL(3),FL(3)
DIMENSION FRQH(4),FRQL(3)
DEFINE AND COMPUTE ALL COEFFICIENTS

UNDER THE PRESENT DATA COLLECTION SYSTEM, 64 SAMPLES ARE TAKEN
PER SECOND. IF ANOTHER DATA COLLECTION SYSTEM IS USED, IT MUST
BE ADJUSTED TO THE SAMPLE PERIOD, I.E., 1/SAMPLE RATE
T=1./64.

COEFFICIENTS FOR FIXED HIGH PASS FILTER
AFHP1=-((T**2/160.-2.)/(1.+T/8.+T**2/320.))
AFHP2=-((1.-T/8.+T**2/320.)/(1.+T/8.+T**2/320.))
BFHP0=(1.)/(1.+T/8.+T**2/320.))
BFHP1=-((2.)/(1.+T/8.+T**2/320.))
BFHP2=(1.)/(1.+T/8.+T**2/320.))
WRITE(6,1002)AFHP1,AFHP2,BFHP0,BFHP1,BFHP2
FORMAT(1X,'FIXED FILTER,AFHP1=,',F19.16,'AFHP2=,',F19.16,'BFHP0=,',
F19.16,'BFHP1=,',F19.16,'BFHP2=,',F19.16)
COEFFICIENTS FOR SELECTABLE HIGH PASS FILTERS

THE FOLLOWING ARRAY VALUES ARE FIXED COEFFICIENTS FOR THE VARIOUS
FREQUENCY SELECTIONS POSSIBLE ON THE AN/ASQ-81
FRQH(1)=0.04
FRQH(2)=0.06
FRQH(3)=0.08
FRQH(4)=0.10
AH(1)=12.52096/40.82834
BH(1)=1./40.82834
CH(1)=1./40.599/45.28317
DH(1)=1./45.28317
EH(1)=7.41498/57.57668
FH(1)=1./57.57668
AH(2)=8.34727/18.14591
BH(2)=1./18.14591
CH(2)=7.33959/20.12587
DH(2)=1./20.12587
EH(2)=4.94332/25.58964
FH(2)=1./25.58964
AH(3)=6.26045/10.20708
BH(3)=1./10.20708
APPL11060
APPL11070
APPL11080
APPL11090
APPL11100
APPL11110
APPL11120
APPL11130
APPL11140
APPL11150
APPL11160
APPL11170
APPL11180
APPL11190
APPL11200
APPL11210
APPL11220
APPL11230
APPL11240
APPL11250
APPL11260
APPL11270
APPL11280
APPL11290
APPL11300
APPL11310
APPL11320
APPL11330
APPL11340
APPL11350
APPL11360
APPL11370
APPL11380
APPL11390
APPL11400
APPL11410
APPL11420
APPL11430
APPL11440
APPL11450
APPL11460
APPL11470
APPL11480
APPL11490
APPL11500
APPL11510
APPL11520
APPL11530

```

```

CH(3)=5.50500/11.32080
DH(3)=1./11.32080
EH(3)=3.70749/14.39417
FH(3)=1./14.39417
AH(4)=5.00836/6.53253
BH(4)=1./6.53253
CH(4)=4.40400/7.24531
DH(4)=1./7.24531
EH(4)=2.96599/9.21227
FH(4)=1./9.21227

```

CCCCCCCC C

```

SELECT THE HIGH PASS FILTER SETTING
FOR THE LOW FREQUENCY CUTOFF AT 0.04 HZ, SET I=1
FOR THE LOW FREQUENCY CUTOFF AT 0.06 HZ, SET I=2
FOR THE LOW FREQUENCY CUTOFF AT 0.08 HZ, SET I=3
FOR THE LOW FREQUENCY CUTOFF AT 0.10 HZ, SET I=4

```

I=1

```

A1=1.+AH(I)*T/2.+BH(I)*(T**2)/4.
B1=-2.+BH(I)*(T**2/2.)*(T**2)/4.
C1=1.-AH(I)*T/2.+BH(I)*(T**2)/4.
D1=1.+CH(I)*T/2.+DH(I)*(T**2)/4.
E1=-2.+CH(I)*(T**2)/2.
F1=1.-CH(I)*T/2.+DH(I)*(T**2)/4.
G1=1.+EH(I)*T/2.+FH(I)*(T**2)/4.
H1=-2.+FH(I)*(T**2)/2.
I1=1.-EH(I)*T/2.+FH(I)*(T**2)/4.

```

CODE IS "ASHP1" MEANS "A1 COEFFICIENT FOR THE SELECTABLE HIGH PASS FILTER"

CCCC

```

ASHP1=1./(A1*D1*G1)
ASHP2=-(C1/A1)
ASHP3=-(B1/A1)
ASHP4=-(E1/D1)
ASHP5=-(F1/D1)
ASHP6=-(H1/G1)
ASHP7=-(I1/G1)

```

WRITE(6,100)FREQH(I),ASHP1,ASHP2,ASHP3,ASHP4,ASHP5,ASHP6,ASHP7
 FORMAT(1X,FREQ=,F5.3,ASHP1=,F19.16,ASHP2=,F19.16,ASHP3=,
 F19.16,ASHP4=,F19.16,/,ASHP5=,F19.16,ASHP6=,F19.16,
 ,ASHP7=,F19.16)

CCCCCCCC

COEFFICIENTS FOR SELECTABLE LOW PASS FILTERS

```

FRQL(1)=0.2
FRQL(2)=0.4

```

```

APP11540
APP11550
APP11560
APP11570
APP11580
APP11590
APP11600
APP11610
APP11620
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APP11640
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APP11670
APP11680
APP11690
APP11700
APP11710
APP11720
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APP11800
APP11810
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APP11900
APP11910
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APP11950
APP11960
APP11970
APP11980
APP11990
APP12000
APP12010

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APP1 2020
 APP1 2030
 APP1 2040
 APP1 2050
 APP1 2060
 APP1 2070
 APP1 2080
 APP1 2090
 APP1 2100
 APP1 2110
 APP1 2120
 APP1 2130
 APP1 2140
 APP1 2150
 APP1 2160
 APP1 2170
 APP1 2180
 APP1 2190
 APP1 2200
 APP1 2210
 APP1 2220
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 APP1 2270
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 APP1 2300
 APP1 2310
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 APP1 2370
 APP1 2380
 APP1 2390
 APP1 2400
 APP1 2410
 APP1 2420
 APP1 2430
 APP1 2440
 APP1 2450
 APP1 2460
 APP1 2470
 APP1 2480
 APP1 2490

FRQL(3)=0.6 C3492 0.03492
 BL(3)=0.358 0.03492
 CL(3)=1.70. C3492
 DL(3)=0.206 0.02779
 EL(3)=1.70. 0.02779
 AL(1)=1.074 1/0. 3143
 CL(1)=1.70. 3143
 DL(1)=0.620 5/0. 2501
 EL(1)=1.70. 2501
 AL(2)=0.537 0.07858
 CL(2)=1.70. 0.07858
 DL(2)=0.310 44/0. 06252
 EL(2)=1.70. 0.06252

SELECT LOW PASS FILTER SETTING AT 0.2 HZ; SET J=1
 FOR THE HIGH FREQUENCY CUTOFF AT 0.4 HZ; SET J=2
 FOR THE HIGH FREQUENCY CUTOFF AT 0.6 HZ; SET J=3

J=3
 A1=AL(J)*(T**2)/4.
 B1=2.
 C1=A1
 D1=DL(J)*(T**2)/4.
 E1=D1
 F1=D1
 G1=(1.2.+CL(J)*T/2.+CL(J)*(T**2)/4.)
 I1=(1.2.+BL(J)*T/2.+CL(J)*(T**2)/4.)
 J1=(1.2.+EL(J)*T/2.+FL(J)*(T**2)/4.)
 K1=(1.2.+FL(J)*T/2.+FL(J)*(T**2)/4.)
 L1=(1.2.+EL(J)*T/2.+FL(J)*(T**2)/4.)
 ASLP1=(G1*K1+H1*J1)/(G1*J1)
 ASLP2=(G1*L1+H1*K1+I1*J1)/(G1*J1)
 ASLP3=(H1*L1+I1*K1)/(G1*J1)
 ASLP4=(I1*L1)/(G1*J1)
 BSLLP0=(A1*D1)/(G1*J1)
 BSLLP1=(A1*E1+B1*DI)/(G1*J1)
 BSLLP2=(A1*F1+B1*EI)/(G1*J1)
 BSLLP3=(B1*F1+C1*EI)/(G1*J1)

CCCCCCC C

```

BSLP4=(C1*F1)/(G1*J1)
WRITE(6,1001)FRQL(J),ASLP1,ASLP2,ASLP3,ASLP4,BSLP0,BSLP1,BSLP2,
$BSLP3,BSLP4
C1001$FORMAT(1X,F19.16,F19.16,F19.16,F19.16,F19.16,F19.16,
$F19.16,/,BSLP0=,F19.16,BSLP1=,F19.16,
$BSLP2=,F19.16,BSLP3=,F19.16,BSLP4=,F19.16)
DO 100 I=1,24576
SIG=ZXXI(1)
YQ=BFHP0*SIG+BFHP1*SIG1+BFHP2*SIG2+AFHP1*YQ1+AFHP2*YQ2
XI=ASHP1*YQ+ASHP2*XI2+ASHP3*XI1
XI1=XI+XI2-2*XI1
XI11=XI1+ASHP4*XI11+ASHP5*XI112
XI1V=XI11-2*XI11+XI112
XV=XIV+ASHP6*XV1+ASHP7*XV2
YQ=XV+XV2-2*XV1
GP1=ASLP1*OUTFD1+ASLP2*OUTFD2+ASLP3*OUTFD3+ASLP4*OUTFD4
GP2=BSLP0*YQ+BSLP1*YQ1+BSLP2*YQ2+BSLP3*YQ3+BSLP4*YQ4
OUTFLD(I)=GP1+GP2
C C C C
FINISHED COMPUTING THIS STEP'S VALUES FOR AMPLITUDES
INCREMENT STORAGE REGISTERS
SIG2=SIG1
SIG1=SIG
YQ2=YQ1
YQ1=YQ
XI2=XI1
XI112=XI11
XI11=XI11
XV1=XV
XV2=XV1
YQ4=YQ3
YQ3=YQ2
YQ2=YQ1
YQ1=YQ
OUTFD4=OUTFD3
OUTFD3=OUTFD2
OUTFD2=OUTFD1
OUTFD1=OUTFLD(1)
C C C
FINISHED INCREMENTING STORAGE REGISTERS
100 CONTINUE
XMAXP=TIME2(16384)
C C
VERSATEC PLOT OF B - FIELD SPECTRA
C C

```

```

C      NPIS=1020./CELTAT +1.
C      NPIS=24576
C      NPIS=0 DETERMINES NUMBER OF POINTS NECESSARY IN ORDER FOR
C      THE 0 TO 2041 SECS RANGE TO BE PLOTTED. REVIEW THE WRITE-UP
C      FOR THE FOLLOWING, ITB, AND RTB, VALUES.
C      FOR THE SUBROUTINE PROCEDURE 'DRAWP'.
      ITB(3)=8
      ITB(4)=4
      ITB(7)=1
      ITB(12)=0
      RTB(1)=0.0
      RTB(2)=0.0
      RTB(3)=ALAB(1)
      READ(5,3000)ITILE
C      DRAW THE COIL ANTENNA TOTAL FIELD DATA SERIES
      CALL DRAWP(NPTS,TIME2,ZZX1,ITB,RTB)
      RTB(3)=ALAB(2)
      READ(5,3000)ITILE
C      DRAW THE ASQ81 TOTAL FIELD DATA SERIES
      CALL DRAWP(NPTS,TIME2,ZZY1,ITB,RTB)
      RTB(3)=ALAB(3)
      READ(5,3000)ITILE
C      DRAW THE SCHONSTEDT COIL FIELD DATA SERIES
      CALL DRAWP(NPTS,TIME2,ZZV1,ITB,RTB)
      RTB(3)=ALAB(4)
      READ(5,3000)ITILE
C      DRAW THE PROGRAM OUTPUT TOTAL FIELD DATA SERIES
      CALL DRAWP(NPTS,TIME2,OUTFLD,ITB,RTB)
      DRAW THE RAW COIL TIME SERIES DATA
      RTB(3)=ALAB(4)
      READ(5,3000)ITILE
      CALL DRAWP(NPTS,TIME2,CLFLD,ITB,RTB)
      CONTINUE
      FORMAT('6A8')
      200 STOP
      3000
C      SUBROUTINE RD(IUN,IO,IRS,IREC,IRQ)

```

```

APP12980
APP12990
APP13000
APP13010
APP13020
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APP13370
APP13380
APP13390
APP13400
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APP13420
APP13430
APP13440
APP13450

```



```

110 IF (IER.EQ.0) GO TO 150
    IRR=IRR+1
    IF (IRR.LT.IRS) GO TO 120
    WRITE(6,110)
    FORMAT('!! STOPPED IN SUB RD BECAUSE OF IRR.GT.',I6,' AT L110.')
    IRR=IRR
    STOP
120 CONTINUE
    WRITE(6,130) IRR, IREC, IRR
    FORMAT('!! RESYNC AT FRAME ',I6,' WITH TOTAL ERRORS ',I7)
    IRR=0
    IREC=0
    GO TO 50
130 CONTINUE
    RETURN
150 IRR=IRR
    IREC=IREC
    WRITE(6,910) IRR, IREC
    FORMAT('!! END OF UNIT ',I3,' AT REC ',I7)
    STOP
    END
C
C
FUNCTION ISHIFT (IN,NPLC)
    RETURNS SHIFTED VALUE OF I*2 WORD IN
    -VE LEFT, +VE RIGHT SHIFT
C
C
INTEGER * 2 IN
IP=IN
IF (IP.LT.0) IP=IP+65536
IF (NPLC.LT.0) GO TO 30
ISHIFT=IP/(2**IABS(NPLC))
RETURN
30 ISHIFT=IP*(2**IABS(NPLC))
IF (ISHIFT.GT.65535) ISHIFT=MOD(ISHIFT,65536)
RETURN
C
C
FUNCTION IMASK (IN,IBL,IBR)
    MASK I*2 WORD IN OUTSIDE BITS IBL & IBR
C
C
INTEGER * 2 IN,IO
IO=IN
IF (IBR.EQ.0) GO TO 50
IT=ISHIFT(IN,IBR)
IO=IT
IP=ISHIFT(IO,IBL-15-IBR)
IO=IP
IMASK=ISHIFT(IO,15-IBL)
RETURN
50 IMASK=IO
END
C
SUBROUTINE FOUR

```

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APPI3940
APPI3950
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APPI3970
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APPI3990
APPI4000
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APPI4070
APPI4080
APPI4090
APPI4100
APPI4110
APPI4120
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APPI4160
APPI4170
APPI4180
APPI4190
APPI4200
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APPI4220
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APPI4290
APPI4300
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PURPOSE

SUBROUTINE FOURT COMPUTES THE FORWARD AND INVERSE COOLEY-TUKEY FAST FOURIER TRANSFORM OF THE CONTENTS OF THE ARRAY DATA. FOR DATA A SINGLY-DIMENSIONED ARRAY OF LENGTH L, THE JTH COMPONENT OF THE TRANSFORM IS GIVEN BY $\sum_{K=1}^L \text{DATA}(K) * W^{JK}$ WHERE THE SUM IS TAKEN OVER K, 1 ≤ K ≤ L, AND $W = \exp(i \cdot 2\pi / L)$.

THE VALUE OF ISIGN DEPENDS UPON WHETHER A FORWARD OR INVERSE TRANSFORM IS TO BE PERFORMED. FOURT MAY ALSO BE USED ON A MULTI-DIMENSIONAL ARRAY, IN WHICH CASE A FOURIER TRANSFORM IS PERFORMED ALONG EACH DIMENSION IN TURN.

CALLING SEQUENCE

CALL FOURT(DATA, NN, NDIM, ISIGN, IFORM, WORK)

DESCRIPTION OF ARGUMENTS

DATA COMPLEX*8 MULTI-DIMENSIONAL ARRAY CONTAINING THE DATA TO BE TRANSFORMED. ON OUTPUT DATA CONTAINS THE TRANSFORM. NORMAL FORTRAN ORDERING IS EXPECTED, THE FIRST SUBSCRIPT CHANGING THE FASTEST.

NN INTEGER*4 ARRAY CONTAINING THE DIMENSIONS OF THE ARRAY DATA.

NDIM NUMBER OF DIMENSIONS OF THE ARRAY DATA = NUMBER OF ELEMENTS IN THE ARRAY NN.

ISIGN INTEGER INDICATING WHETHER FORWARD OR INVERSE TRANSFORM IS TO BE PERFORMED.

ISIGN = -1 FOR FORWARD TRANSFORM
 ISIGN = 1 FOR INVERSE TRANSFORM.
 NOTE: THESE DEFINITIONS ARE NOT STANDARDIZED. IN PARTICULAR, THE DEFINITIONS OF FORWARD AND INVERSE TRANSFORM ARE REVERSED IN THE IMSL FFT ROUTINES.

IFORM AN INTEGER INDICATING WHETHER OR NOT DATA CONTAINS ONLY PURELY REAL VALUES.

IFORM = 0 IF DATA IS PURELY REAL
 IFORM = 1 OTHERWISE.

IF IFORM IS SET TO 0, ALL THE IMAGINARY PARTS OF THE ELEMENTS IN DATA MUST BE SET TO 0.0.


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WORK A 1-DIMENSIONAL REAL*4 ARRAY USED FOR WORKING STORAGE.
 ITS LENGTH SHOULD BE TWICE THE LARGEST ARRAY OF DIMENSION
 NN(1), I=1,2 IF...NDIM, WHICH IS NOT A POWER OF TWO. IN
 PARTICULAR, IF ALL NN(I) ARE POWERS OF TWO, NO WORK SPACE
 IS NEEDED AND WORK MAY BE REPLACED BY ZERO IN THE CALLING
 SEQUENCE.

REMARKS

IF AN INVERSE TRANSFORM (ISIGN=+1) IS PERFORMED UPON AN ARRAY
 OF TRANSFORMED (ISIGN=-1) DATA, THE ORIGINAL DATA WILL REAP-
 PEAR, MULTIPLIED BY NN(1)*NN(2)*...*NN(NDIM).

FOR A MULTI-DIMENSIONAL ARRAY THE (J1,J2,...,JNDIM)
 COMPONENT OF THE TRANSFORM IS GIVEN BY
 SUM(DATA(I1,I2,...,INDIM)*W1**((I1-1)*(J1-1)))*
 W2**((I2-1)*(J2-1))*...*WNDIM**((INDIM-1)*(JNDIM-1))
 HERE THE SUM RANGES OVER ALL POSSIBLE VALUES OF THE I'S
 AND W1=EXP(ISIGN*2*PI*SQRT((-1)/NN(1)), ETC.

THE ARRAY OF INPUT DATA MUST BE IN COMPLEX FORMAT.
 HOWEVER, IS ALL IMAGINARY PARTS ARE ZERO (I.E., FORTY PER-
 CENT. (FOR FASTEST TRANSFORM OF REAL DATA, NN(1) SHOULD BE E-
 VEN.) THE TRANSFORM VALUES ARE ALWAYS COMPLEX AND ARE RETURNED
 IN THE ORIGINAL DIMENSION OF THE DATA. THE INPUT DATA, THE
 LENGTH OF EACH DIMENSION OF THE DATA ARRAY MAY BE ANY INTEGER.
 THE PROGRAM RUNS FASTER ON COMPOSITE INTEGERS THAN ON PRIMES,
 AND IS PARTICULARLY FAST ON NUMBERS RICH IN FACTORS OF TWO.

TIMEING IS IN FACT GIVEN BY THE FOLLOWING FORMULA. LET NOT BE
 THE TOTAL NUMBER OF POINTS (REAL OR COMPLEX) IN THE DATA ARRAY.
 THAT IS, NOT=NN(1)*NN(2)*...*NN(K3)*5**K5*...SUMF=2*K2. LET
 FACTORS, SUCH AS 2**K2*3**K3*5**K5*...SUMF=2*K2. LET
 SUMF BE THE SUM OF ALL OTHER FACTORS OF NOT, THAT IS, SUMF=2
 3*K3*5*K5*. THE TIME TO ADD NOT*(I1+I2*SUM2+I3*SUMF) ON THE
 THESE NOT. DATA IS POINT ADD TIME = SIX MICROSECONDS). T = 3000+
 CDC 3300 (FLOATING POINT ADD TIME = SIX MICROSECONDS). T = 3000+
 NOT*(600+40*SUM2+175*SUMF) MICROSECONDS ON COMPLEX DATA.

THE SAVINGS OFFERED BY THIS PROGRAM CAN BE DRAMATIC. A ONE-DI-
 MENSIONAL ARRAY 4000 IN LENGTH WILL BE TRANSFORMED IN 4000*(600+
 40*(2+2+2+2)+175*(5+5+5)) = 14.5 SECONDS VERSUS ABOUT 4000*
 4000*175 = 2800 SECONDS FOR THE STRAIGHTFORWARD TECHNIQUE.

THE FAST FOURIER TRANSFORM PLACES THREE RESTRICTIONS UPON THE
 DATA.

1. THE NUMBER OF INPUT DATA AND THE NUMBER OF TRANSFORM VALUES MUST BE THE SAME.
2. BOTH THE INPUT DATA AND THE TRANSFORM VALUES MUST REPRESENT EQUISPACED POINTS IN THESE RESPECTIVE DOMAINS OF TIME AND FREQUENCY. CALLING DELTAF=2*PI/(NN(I)*DELTAT), IT MUST BE TRUE THAT DELTAF=2*PI/(NN(I)*DELTAT). OF COURSE, DELTAT NEED NOT BE THE SAME FOR EVERY DIMENSION.
3. CONCEPTUALLY AT LEAST, THE INPUT DATA AND THE TRANSFORM OUTPUT REPRESENT SINGLE CYCLES OF PERIODIC FUNCTIONS.

THERE ARE NO ERROR MESSAGES OR ERROR HALTS IN THIS PROGRAM. THE PROGRAM RETURNS IMMEDIATELY IF NDIM OR ANY NN(I) IS LESS THAN ONE.

FOR MOST APPLICATIONS FOURT, IF COMPILED UNDER FORTRAN H, IS COMPARABLE IN SPEED AND ACCURACY TO THE IMSL FFT SUBROUTINES. WITH CERTAIN PATHOLOGICALLY ILL-CONDITIONED DATA THE ACCURACY OF FOURT MAY BE SERIOUSLY DEGRADED, BUT THE SAME CAN PROBABLY BE SAID OF ANY EXTANT FFT ROUTINE. WORK SPACE REQUIRED BY FOURT MAY BE GREATER OR LESS THAN THAT REQUIRED BY THE IMSL ROUTINES, DEPENDING UPON THE APPLICATION. FOURT IS MORE FLEXIBLE AND IN GENERAL EASIER TO USE THAN THE IMSL ROUTINES. FOURT ALONE PROVIDES THE CAPABILITY OF TRANSFORMING A MULTI-DIMENSIONAL ARRAY WITH A SINGLE CALL.

THIS IS THE FASTEST AND MOST VERSATILE VERSION OF THE FFT KNOWN TO THE AUTHOR. A PROGRAM CALLED FOUR2 IS AVAILABLE THAT ALSO PERFORMS THE FAST FOURIER TRANSFORM AND IS WRITTEN IN USASIBASIC FORTRAN. IT IS ABOUT ONE THIRD AS LONG AND REQUIRES THE DIMENSIONS OF THE INPUT ARRAY (WHICH MUST BE COMPLEX) TO BE POWERS OF TWO. ANOTHER PROGRAM, CALLED FOUR1, IS ONE TENTH AS LONG AND RUNS TWO THIRDS AS FAST ON A ONE-DIMENSIONAL COMPLEX ARRAY WHOSE LENGTH IS A POWER OF TWO.

REFERENCE--

IEEE AUDIO TRANSACTIONS (JUNE 1967), SPECIAL ISSUE ON THE FFT.

EXAMPLE 1. THREE-DIMENSIONAL FORWARD FOURIER TRANSFORM OF A COMPLEX ARRAY DIMENSIONED 32 BY 25 BY 13 IN FORTRAN IV.

```

DIMENSION DATA(32,25,13),WORK(50),NN(3)
COMPLEX DATA
DATA NN/32,25,13/
DO 1 I=1,32
DO 1 J=1,25
DO 1 K=1,13
DATA(I,J,K)=COMPLEX VALUE
CALL FOURT(DATA,NN,3,-1,1,WORK)

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2  CCCCCCCCCCCCCCCCCC
3  CCCCCCCCCCCCCCCCCC
4  CCCCCCCCCCCCCCCCCC
5  CCCCCCCCCCCCCCCCCC
6  CCCCCCCCCCCCCCCCCC
7  CCCCCCCCCCCCCCCCCC
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9  CCCCCCCCCCCCCCCCCC
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EXAMPLE 2. ONE-DIMENSIONAL FORWARD TRANSFORM OF A REAL ARRAY OF
 LENGTH 64 IN FORTRAN II
 DIMENSION DATA(2,64)
 DO 2 I=1,64
 DATA(1,I)=REAL PART
 DATA(2,I)=0
 CALL FOURT(DATA,64,1,-1,0,0)
 PROGRAMMER
 PROGRAM BY NORMAN BRENNER FROM THE BASIC PROGRAM BY CHARLES
 RADER, JUNE 1967. THE IDEA FOR THE DIGIT REVERSAL WAS
 SUGGESTED BY RALPH ALTER.
 DOCUMENTATION REVISED BY JOANNE BOGART, AUGUST 1979, NPS.
 SUBROUTINE FOURT(DATA,NN,NDIM,ISIGN,IFORM,WORK,
 DIMENSION DATA(1),NN(1),IFACT(32),WORK(1)
 DATA TWOPI/6.2831853071796/.RTHLF/0.70710678118655/
 IF(NDIM-1)920,1,1
 NTOT=2
 DO 2 I DIM=1,NDIM
 IF(NN(I)920,920,2
 NTOT=NTOT*NN(I)
 MAIN LOOP FOR EACH DIMENSION
 NP1=2
 DO 910 IDIM=1,NDIM
 N=NN(IDIM)
 NP2=NP1*N
 IF(N-1)920,900,5
 IS N A POWER OF TWO AND IF NOT, WHAT ARE ITS FACTORS
 M=N
 NTWO=NP1
 IF=1
 IDIV=2
 IQUOT=M/IDIV
 IREM=N-IDIV*IQUOT
 IF(IQUOT-IDIV)50,1,1,1
 IF(IREM)20,12,20
 NTWO=NTWO+N IWO
 IFACT(I)=IDIV
 IF=IF+1
 M=IQUOT
 GO TO 10
 IDIV=3

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30      INQN2=IF
      IQUOT=M/IDIV
      IREM=M-IDIV*IQUOT
31      IF(IQUOT-IDIV)60,31,31
32      IF(IREM)40,32,40
      IFACT(I)=IDIV
      IF=IF+1
      M=IQUOT
      GO TO 30
40      IDIV=IDIV+2
      GO TO 30
50      INQN2=IF
      IF(IREM)60,51,60
51      NTWO=NTWO+NTWO
      GO TO 70
60      IFACT(I)=M

      SEPARATE FOUR CASES--
      1. COMPLEX TRANSFORM OR REAL TRANSFORM FOR THE 4TH, 9TH, ETC.
          DIMENSIONS
      2. REAL TRANSFORM FOR THE 2ND OR 3RD DIMENSION. METHOD--
          TRANSFORM HALF THE DATA, SUPPLYING THE OTHER HALF BY CON-
          JUGATE SYMMETRY.
      3. REAL TRANSFORM FOR THE 1ST DIMENSION, N ODD. METHOD--
          SET THE IMAGINARY PARTS TO ZERO.
      4. REAL TRANSFORM FOR THE 1ST DIMENSION, N EVEN. METHOD--
          TRANSFORM A COMPLEXED REAL ARRAY OF LENGTH N/2 WHOSE REAL PARTS
          ARE THE EVEN NUMBERED REAL VALUES AND WHOSE IMAGINARY
          PARTS ARE THE ODD NUMBERED REAL VALUES. SEPARATE AND SUP-
          PLY THE SECOND HALF BY CONJUGATE SYMMETRY.

70      ICASE=1
      IFMIN=1
      IIRNG=NP1
      IF(IDIM-1)71,100,100
      IF(IIFORM)72,72,100
71      ICASE=2
72      IIRNG=NP0*(1+NPREV/2)
      IF(IDIM-1)73,73,100
      ICASE=3
73      IIRNG=NP1
      IF(NTWO-NP1)100,100,74
74      ICASE=4
      IFMIN=4
      NTWO=NTWO/2
      NP2=NP2/2
      NTOT=NTOT/2

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      I=1      80      J=1,NTOT
      DO DATA(J)=DATA(I)
      I=I+2
C
C
C
      SHUFFLE DATA BY BIT REVERSAL, SINCE N=2**K. AS THE SHUFFLING
      CAN BE DONE BY SIMPLE INTERCHANGE, NO WORKING ARRAY IS NEEDED
C
      IF (NTWO-NP2)200,110,110
      NP2HF=NP2/2
      J=1
      DO 150 I2=1,NP2,NP1
      IF (J-I2)120,130,130
      I1MAX=I2+NP1-2
      DO 125 I1=I2,11MAX,2
      DO 125 I3=11,NTOT,NP2
      J3=J+I3-12
      TEMPR=DATA(I3)
      TEMPI=DATA(I3+1)
      DATA(I3)=DATA(J3+1)
      DATA(J3)=TEMPR
      DATA(J3+1)=TEMPI
      M=NP2HF
      IF (J-M)150,150,145
      J=J-M
      M=M/2
      IF (M-NP1)150,140,140
      J=J+M
      GO TO 300
C
C
C
      SHUFFLE DATA BY DIGIT REVERSAL FOR GENERAL NG ARRAY IS NEEDED
C
      NWORK=2*N
      DO 270 I1=1,NP1,2
      DO 270 I3=11,NTOT,NP2
      J=I3
      DO 260 I=1,NWORK,2
      IF (ICASE-3)210,220,210
      WORK(I)=DATA(J)
      WORK(I+1)=DATA(J+1)
      GO TO 230
      WORK(I)=DATA(J)
      WORK(I+1)=0.
      IF P2=NP2
      IF P2=MIN
      IF P1=IFP2/IFACT(IF)
      J=J+1IFP1
      200
      210
      220
      230
      240
  
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420 DO 530 I1=1,I1RNG,2
      KM IN=I1+IPAR*M
      IF (MMAX-NP1)430,430,440
430 KM IN=I1
440 KD IF=IPAR*MMAX
450 KSTEP=4*KDIF
460 IF (KSTEP-NP1)460,460,530
      DO 520 K1=KMIN,NTOT,KSTEP
        K2=K1+KDIF
        K3=K2+KDIF
        K4=K3+KDIF
        IF (MMAX-NP1)470,470,480
470 U1R=DATA(K1)+DATA(K2)
          U2R=DATA(K1)+DATA(K3)
          U2I=DATA(K3)+DATA(K4)
          U3R=DATA(K1)+DATA(K2)
          U3I=DATA(K1)+DATA(K3)
          IF (ISIGN)471,472,472
471 U4R=DATA(K3)+DATA(K4)
          U4I=DATA(K3)-DATA(K4)
          GO TO 510
472 U4R=DATA(K4+1)-DATA(K3+1)
          U4I=DATA(K3)-DATA(K4)
          GO TO 510
480 T2R=W2R*DATA(K2)+W2I*DATA(K2+1)
          T3R=W2R*DATA(K3)+W2I*DATA(K3+1)
          T3I=W2R*DATA(K3)+W2I*DATA(K4)
          T4R=W3R*DATA(K4)+W3I*DATA(K4+1)
          T4I=W3R*DATA(K4)+W3I*DATA(K4)
          U1R=DATA(K1)+T2R
          U1I=DATA(K1)+T2I
          U2R=DATA(K1)+T4R
          U2I=DATA(K1)+T4I
          U3R=DATA(K1)+T2R
          U3I=DATA(K1)+T2I
          IF (ISIGN)490,490,500
490 U4R=DATA(K1)+T4R
          U4I=DATA(K1)+T4I
          GO TO 510
500 U4R=DATA(K1)+T4R
          U4I=DATA(K1)+T4I
510 DATA(K1)=U1R+U2R
          DATA(K1+1)=U3R+U4R
          DATA(K2)=U3I+U4I
          DATA(K3)=U1R+U2R

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520 DATA(K3+1)=U11-U21
    DATA(K4)=U3R-U4R
    DATA(K4+1)=U31-U41
    KDIF=KSTEP
    KMIN=4*(KMIN-11)+11
    GO TO 450
530 CONTINUE
    M=M+LMAX
    IF(M-MMAX)540,540,570
540 IF((SIGN)550,560,560
550 TEMPR=WR
    WR=(WR+WI)*RTHLF
    WI=(WI-TEMPR)*RTHLF
    GO TO 410
560 TEMPR=WR
    WR=(WR-WI)*RTHLF
    WI=(TEMPR+WI)*RTHLF
    GO TO 410
570 CONTINUE
    IPAR=3-IPAR
    MMAX=MMAX+MMAX
    GO TO 360

C C C C C
    MAIN LOOP FOR FACTORS NOT EQUAL TO TWO. APPLY THE TWIDDLE FAC-
    TOR W=EXP(I*SIGN*2*PI*SQRT(-1))*(J1-1)/(J2-J1)/(IFP1+IFP2)),
    THEN PERFORM A FOURIER TRANSFORM OF LENGTH IFACT(IF), MAKING USE
    OF CONJUGATE SYMMETRIES.
    IF(NTWO-NP2)605,700,700
    IFP1=NTWO
    IF=INON2
    NP1HF=NP1/2
    IFP2=IFACT(IF)*IFP1
    J1MIN=NP1+1
    IF(J1MIN-IFP1)615,615,640
    DO 635 J1=J1MIN,IFP1,NP1
    THETA=-TWOPI*FLOAT(J1-1)/FLOAT(IFP2)
    IF((SIGN)625,620,620
    THETA=-THETA
    WSTPR=COS(THETA)
    WSTPI=SIN(THETA)
    WR=WSTPR
    WI=WSTPI
    J2MIN=J1+IFP1
    J2MAX=J1+IFP2-IFP1
    DO 635 J2=J2MIN,J2MAX,IFP1
    I1MAX=J2+I1RNG-2
    DO 630 I1=J2,I1MAX,2

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APP19110
APP19120
APP19130
APP19140
APP19150
APP19160
APP19170
APP19180
APP19190
APP19200
APP19210

```

630      J3=I1,NTOT,IFP2
        TEMPR=DATA(J3)
        DATA(J3)=DATA(J3)*WR-DATA(J3+1)*WI
        DATA(J3+1)=TEMPR*WI+DATA(J3+1)*WR
        TEMPR=WR
        WI=WR*WSTPR-WI*WSTPI
        THEIA=-TWOPI/FLQAT(IFACT(IF))
        IF(ISIGN)650,645,645
        THEIPR=-THEIA
        WSTPI=COSE(THEIA)
        WSTRNG=IFPI*(1+IFACT(IF)/2)
        DO 695      I1=1,11,IRNG,2
        DO 695      I3=1,1,NTOT,NP2
        J2MAX=I3+J2RNG-IFP1
        DO 690      J2=I3,J2MAX,IFP1
        J1MAX=J2+IFP1-NP1
        DO 680      J1=J2,J1MAX,NP1
        J3MAX=J1+NP2-IFP2
        DO 680      J3=J1,J3MAX,IFP2
        JMIN=J3-J2+I3
        JMAX=JMIN+IFP2-IFP1
        I=1+(J3-I3)/NP1HF
        IF(J2-I3)655,665,665
        SUMR=0.
        SUMI=0.
        DO 660      J=JMIN,JMAX,IFP1
        SUMR=SUMR+DATA(J)
        SUMI=SUMI+DATA(J+1)
        WORK(I)=SUMR
        WORK(I+1)=SUMI
        GO TO 680
        ICONJ=1+(IFP2-2*J2+I3+J3)/NP1HF
        J=JMAX
        SUMR=DATA(J)
        SUMI=DATA(J+1)
        OLDSR=0.
        OLDSI=0.
        J=J-IFP1
        TEMPR=SUMR
        SUMPR=TWOWR*SUMR-OLDSR+DATA(J)
        TEMPI=SUMI
        SUMPI=TWOWR*SUMI-OLDSI+DATA(J+1)
        OLDSR=TEMPR
        OLDSI=TEMPI
        J=J-IFP1
        IF(J-JMIN)675,675,670

```

```

675 TEMPR=WR*SUMR-OLDSR+DATA(J)
    TEMPI=WI*SUMI
    WORK(I)=TEMPR-TEMPI
    WORK(I*CONJ)=TEMPR+TEMPI
    TEMPR=WR*SUMR-OLDSI+DATA(J+1)
    TEMPI=WI*SUMI
    WORK(I+1)=TEMPR+TEMPI
    WORK(I*CONJ+1)=TEMPR-TEMPI
    CONTINUE
    IF(J2-I3)685,685,686
680 IF(J2-I3)685,685,686
685 WR=WSTPI
    WI=WI*CONJ
    GO TO 690
686 TEMPR=WR
    WR=WR*WSTPI-WI*WSTPI
    WI=TEMPR*WSTPI+WI*WSTPI
690 TQWR=WR+WI
    I=1
    I2MAX=I3+NP2-NP1
    DO 695 I2=I3,I2MAX,NP1
    DATA(I2)=WORK(I)
    DATA(I2+1)=WORK(I+1)
    I=I+2
    IF=IF+1
    IFPI=IF*P2
    IF(1-IFPI-NP2)610,700,700
    COMPLETE A REAL TRANSFORM IN THE 1ST DIMENSION, N EVEN, BY CON-
    JUGATE SYMMETRIES.
    GO TO (900,800,900,701),ICASE
700 NHALF=N
701 N=NH+N
    THETA=-TWOPI/FLOAT(N)
    IF(1-IGN)703,702,702
    THETA=-THETA
    WSTPI=CONJ(THETA)
    WSTPI=SIN(THETA)
    WR=WSTPI
    WI=WSTPI
    IMIN=3
    JMIN=2*NHALF-1
    GO TO 725
710 J=JMIN
    DO 720 I=IMIN,NTOT,NP2
    SUMR=(DATA(I)+DATA(J))/2.
    SUMI=(DATA(I+1)+DATA(J+1))/2.
    DIFR=(DATA(I)-DATA(J))/2.

```

```

720  DIFI=(DATA(I+1)-DATA(J+1))/2.
      TEMPR=WR*SUMI+WI*DIK
      TEMPI=WI*SUMI-WR*DIK
      DATA(I)=SUMR+TEMPR
      DATA(I+1)=DIK+TEMPI
      DATA(J)=SUMR-TEMPR
      DATA(J+1)=-DIK+TEMPI
      J=J+NP2
      IMIN=IMIN+2
      JMIN=JMIN-2
      TEMPR=WR
      WR=WR*WSTPR-WI*WSTPI
      WI=TEMPR+WSI*WSTPI
      IF(I=JMIN)JMIN=J+1
      IF(I=JMIN)JMIN=J+1
      DO I=JMIN, J+1
        DATA(I)=DATA(I+1)
        NP2=NP2+NP2
        NTOT=NTOT+NP2
        J=J+1
        IMIN=IMIN+1
        I=I+1
        GO TO 755
      DATA(J)=DATA(I)
      DATA(J+1)=-DATA(I+1)
      I=I+2
      J=J-2
      IF(I=JMIN)JMIN=J+1
      DATA(J)=DATA(I)
      DATA(J+1)=DATA(I+1)
      IF(I=JMIN)JMIN=J+1
      DATA(J)=DATA(I)
      DATA(J+1)=DATA(I+1)
      I=I-2
      J=J-2
      IF(I=JMIN)JMIN=J+1
      DATA(J)=DATA(I)
      DATA(J+1)=DATA(I+1)
      IMAX=IMIN
      GO TO 745
      DATA(1)=DATA(1)+DATA(2)
      DATA(2)=0.
      GO TO 900
      COMPLETE A REAL TRANSFORM FOR THE 2ND OR 3RD DIMENSION BY
      CONJUGATE SYMMETRIES.
      IF(I=JMIN)JMIN=J+1
      GO TO 800

```

```

805      DO 860 I3=1,NTOT,NP2
      I2MAX=I3+NP2-NP1
      DO 860 I2=I3,I2MAX,NP1
      IMIN=I2+IIRNG
      IMAX=I2+NP1-2
      IF (I2-I3)820,820,810
      JMAX=JMAX+NP2
      IF (IDIM-2)850,850,830
      J=JMAX*NP0
      DO 840 I=IMIN,IMAX,2
      DATA(I)=DATA(J)
      DATA(I+1)=-DATA(J+1)
      J=J-2
      J=JMAX
      DO 860 I=IMIN,IMAX,NP0
      DATA(I)=DATA(J)
      DATA(I+1)=-DATA(J+1)
      J=J-NP0
      END OF LOOP ON EACH DIMENSION
      C
      C
      NP0=NP1
      NP1=NP2
      NPREV=N
      RETURN
      END
/*GD*SYSIN DD *
LA MESA VILLAGE, 13 MAY 83
COIL ANTENNA AMP IN NT 13 MAY 83
LA MESA VILLAGE, 13 MAY 83
ASQ-81 AMP IN NT 13 MAY 83
LA MESA VILLAGE, 13 MAY 83
FLUXGATE VILLAGE, 13 MAY 83
LA MESA VILLAGE, 13 MAY 83
PRUGRAM OUTPUT IN NT 13 MAY 83
LA MESA VILLAGE, 13 MAY 83
RAW COIL VILLAGE, 13 MAY 83
LA MESA VILLAGE, 13 MAY 83
COIL ANTENNA AMP IN NT 13 MAY 83
LA MESA VILLAGE, 13 MAY 83
ASQ81 AMP IN NT 13 MAY 83
LA MESA VILLAGE, 13 MAY 83
FLUXGATE VILLAGE, 13 MAY 83
LA MESA VILLAGE, 13 MAY 83
PRUGRAM OUTPUT IN NT 13 MAY 83
LA MESA VILLAGE, 13 MAY 83

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APP20640
APP20650

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APP20660
APP20670
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APP20690
APP20700
APP20710

RAW COIL TIME SERIES IN VOLTS
/*
//GO.FT20F001 DD UNIT=3400-4,VOL=SER=MIKE1,DISP=(OLD,KEEP),
// LABEL=(1,NL,IN)
// DCB=(RECFM=FB,LRCL=32,BLKSIZE=512,DEN=2)
//GO.SYSDUMP DD SYSOUT=A,OUTLIM=65000

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